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# COMPUTER PROGRAM FOR STEADY TRANSONIC FLOW OVER THIN AIRFOILS BY FINITE ELEMENTS

HUNTSVILLE RESEARCH & ENGINEERING CENTER LOCKHEED MISSILES & SPACE COMPANY, INC.

OCTOBER 1975

TECHNICAL REPORT AFFDL-TR-75-126
REPORT FOR PERIOD APRIL 1975 — JUNE 1975



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ABSTRACT (Continue on reverse side if necessary and identify by block number) A finite element program is described for the analysis of subsonic and transonic flows over thin airfoils by solving the nonlinear transonic potential equation based on small disturbance theory. The present numerical algorithm is developed using the concept of finite elements in conjunction with the least square method of weighted residuals. Since the governing equation is of the elliptic-hyperbolic type, a none-sided assembly technique was devised and adapted in the supersonic region to restore the directional property of the flow, which was removed by the exclusion of entropy from the transonic potential equation. The finite element discretization results in a system of banded nonlinear algebraic equations, which is solved by direct iterations. The elements presently used include triangles and quadrilaterals with the perturbed potential function and velocity components as nodal unknowns. Boundary conditions of both Dirichlet and Neumann types are therefore imposed conveniently. Also, secondary unknowns, such as local Mach number and pressure coefficient, etc., are computed directly without resorting to numerical differentiation. The present computer program is separated into two parts: the first part (designated as STRANL-I) generates; from a limited number of input cards, the necessary mesh information and, if desired, produces a mesh plot and optimal nodal numbering as well; the second part (STRANL-II) carries out the analysis and displays the pressure coefficients along the chord line on printer plots. Two sample cases of flow over a NACA 64 A006 and a 6% thick circular arc are given to demonstrate the applicability and usage of the program. The solution procedures are found to be very accurate and quite efficient, permitting the aerodynamic forces to be calculated to engineering accuracy in tens of seconds on a CDC 6600 computer.

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### FOREWORD

This report was prepared by personnel in the Computational Mechanics Section of the Lockheed Missiles & Space Company, Inc., Huntsville Research & Engineering Center, Huntsville, Alabama for the Air Force Flight Dynamics Laboratory, Wright-Patterson Air Force Base, Ohio. The computer programs were developed under Project 1370, "Dynamic Problems in Flight Vehicles," Task 137004, "Design Analysis," Contract F33615-75-C-3125. Capt. Gerald Van Keuren, AFFDL/FYS, is the Air Force Project Engineer.

S.T.K. Chan was the principal investigator for the study including computer program development under the supervision of M.R. Brashears. The authors are grateful for the assistance of the following Lockheed-Huntsville personnel: V.Y.C. Young, for the invaluable technical discussions and A.J. Jordan for aid in computer program conversion.

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# LIST OF SYMBOLS

Symbol	
a	local speed of sound
С	chord length of airfoil
$^{\mathrm{C}}_{\mathrm{p}}$	pressure coefficient
g (x)	thickness distribution of the airfoil
<sup>L</sup> i	right-hand side vector of the resulting system of equations
M = V/a	local Mach number
$^{ m M}_{\infty}$	freestream Mach number
$N_{\mathbf{i}}$	shape functions
p	local static pressure
$P_{O}$	stagnation pressure
R	residual resulting from any approximate solution
$\mathtt{s}_{\mathbf{i}\mathbf{j}}$	system coefficient matrix
u, v	perturbed velocity components in the x- and y-directions, respectively
$^{\mathrm{U}}_{\infty}$	freestream speed
x = x'/c $y = y'/c$	nondimensional $x$ and $y$ coordinates
Greek	
γ	ratio of specifc heats ( $\gamma$ = 1.4 for air)
$\epsilon$	small number used as convergence criterion
θ	under-relaxation factor
$\phi = \phi' / (U_{\infty} \cdot c)$	nondimensional perturbation velocity potential
$\phi_{f i}$	undetermined parameters at nodal points
X	integral expression for the squared errors over the entire flow domain

In addition, a repeated index implies summation unless specified otherwise. Also, subscripts after a comma indicate partial differentiations.

gradient of a scalar function

 $\nabla$ 

# 1. INTRODUCTION

The aim of the present study was to develop an efficient and accurate numerical algorithm for the analysis of steady transonic flow over nonlifting thin airfoils. With this objective, the present formulation is therefore based on the small disturbance but nonlinear transonic potential equation for inviscid, compressible fluid.

It is well known that two major difficulties exist in solving the transonic flow problem: (1) the governing partial differential equation is nonlinear, and (2) the equation is of mixed elliptic-hyperbolic type. Because of these difficulties, numerical procedures must therefore be used, with provisions made to properly account for the above transonic effects. Among the numerical approaches, the finite difference relaxation technique is the most well developed and widely used in recent transonic calculations. On the other hand, the finite element technique, in spite of its tremendous success in the field of solid and structural mechanics, has never been attempted until the present investigation, obviously because conventional finite element technique is invalid in solving mixed-type equations. This difficulty, nevertheless, was successfully resolved by a special assembling technique devised for the supersonic region, while the major advantages of the conventional finite element method are retained. These include the complete flexibility in element arrangement, its effectiveness to cope with complex geometric shapes and boundary conditions, and the ease with using efficient higher order approximations. For these reasons, the present approach appears to be superior in solution accuracy and computational efficiency compared to other existing numerical techniques.

The present numerical algorithm is developed using the concept of finite elements in conjunction with the least squares method of weighted residuals

The basic element presently used has a cubic expansion for the perturbed velocity potential inside the element, with nodal unknowns representing the function itself and the two perturbed velocity components. The resulting system of nonlinear algebraic equations is banded, although non-symmetric. This system of algebraic equations is solved by direct iterative procedures.

The theory and numerical procedures, together with the usage of the computer programs, are discussed in the following sections. The theory including the small disturbance potential equation with its corresponding boundary conditions and the related secondary unknowns are summarized in Section 2. The numerical procedures employed in the present approach are discussed in Section 3. These include the finite element formulation based on least squares, elements used in the computation, special considerations for the supersonic region, treatment of boundary conditions and a description of the iterative procedures. In Section 4, the two parts of the computer code, namely, STRANL-I and STRANL-II are described separately, in the aspects of scope and flow chart, description of variables, subroutines used, and finally input and output. Two sample cases are given in Section 5 to demonstrate how to use these computer programs, which are listed in the Appendixes.

### 2. THEORY - ASSUMPTIONS AND BASIC EQUATIONS

The objective of the present study was to develop an efficient and accurate numerical algorithm for the analysis of steady transonic flow over nonlifting thin airfoils. With this objective in mind, the formulation was therefore based on the small disturbance but nonlinear transonic potential equation for inviscid, compressible fluid. The embedded shock is assumed to be weak and boundary layer effects are neglected. These assumptions render the small perturbation theory possible and lead to the following mathematical problem to be solved.

### Differential Equation

$$\left[1 - M_{\infty}^{2} - M_{\infty}^{2} (1 + \gamma) \phi_{,x}\right] \phi_{,xx} + \phi_{,yy} = 0 \qquad (1)$$

# Boundary Conditions

$$(1 + u) \frac{dg}{dx} - v = 0$$
 on the airfoil (2)

$$\nabla \phi = 0 \qquad \text{at infinity} \tag{3}$$

$$v = 0$$
 on line of symmetry (4)

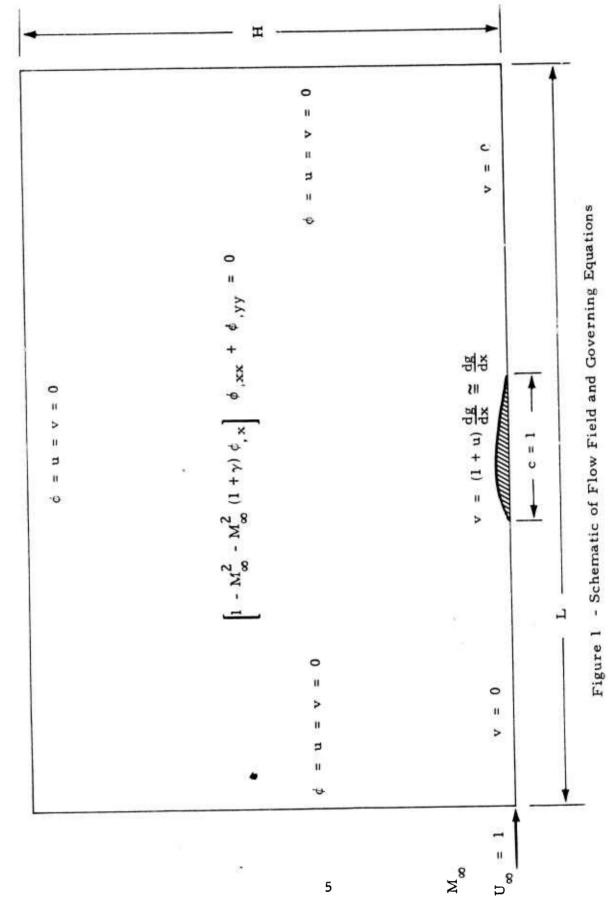
where  $\phi$  = perturbed velocity potential function, u,v = perturbed velocity components in the x- and y-directions, respectively,  $M_{\infty}$  = freestream Mach number,  $\gamma$  = ratio of specific heats, taken to be 1.4 for air, and g = function of x defining the geometry of the airfoil. Equation (1) is in dimensionless form and the

x-axis is aligned with the undisturbed flow direction. The dimensional (with primes) and nondimensional quantities are related by

$$x = \frac{x'}{c}$$
,  $y = \frac{y'}{c}$  and  $\phi = \frac{\phi'}{U_{\infty}c}$ 

where c and  $U_{\infty}$  are the characteristic length and speed, which are currently taken as the chord length and the freestream speed, respectively.

Figure 1 shows the flow field, together with the steady transonic governing equation and corresponding boundary conditions. Because only nonlifting thin airfoils are being considered, the airfoils are necessarily symmetric and hence only half of the flow field is depicted and analyzed. As the figure shows, the flow tangency condition on the airfoil is retained in its nonlinear form, as defined by Eq. (2), and is to be applied along the actual airfoil surface. Another approach is to use the linearized boundary condition and apply it along the airfoil chordline, as commonly adapted in most existing finite difference codes. Apparently, use of the nonlinear form is more accurate when the magnitude of u becomes non-negligible. On the other hand, use of the linearized boundary condition could enhance solution convergence somewhat as the nonlinearity now exists in the governing equation only. Extensive studies and comparisons are certainly required in order to assess the two approaches. In the present computer code, the nonlinear form is used unless otherwise specified through an input control key, in which case the linear form will be used. On the line of symmetry, as is well known, the Neumann condition of no normal flow is to be imposed. For the far field, because only a finite domain can be treated in the analysis, the condition of no disturbance at infinity is assumed to be valid on the outer boundary which is usually taken as a few chord lengths away from the airfoil. Numerical experimentations indicate that a flow region with  $H \ge 2c$  and  $L \ge 4c$  is generally required to yield solution with adequate accuracy. For flow with higher freestream Mach number, the flow region should be extended somewhat to account for effects from the enlarging supersonic pocket.



For the problem of lifting airfoils, the entire flow domain must be considered. In this case, an asymptotic solution including at least the circulation as unknown should be applied on the finite outer boundary. This is part of a current study conducted for AFFDL and will be implemented later.

Once the flowfield solution in terms of the perturbed velocity potential has been obtained, all secondary unknowns can be calculated subsequently.

These include

$$a = \left[\frac{\gamma - 1}{2} (U_{\infty}^2 - V^2) + (\frac{U_{\infty}}{M_{\infty}})^2\right]^{1/2}$$
 (5)

$$M = \frac{V}{a} \tag{6}$$

$$\frac{p}{p_o} = \frac{1}{\left[1 + \frac{\gamma + 1}{2} M^2\right] \frac{\gamma}{\gamma - 1}} \tag{7}$$

$$C_p = -\left[\frac{2u}{U_{\infty}} + (1 - M_{\infty}^2) \frac{u^2}{U_{\infty}^2} + \frac{v^2}{U_{\infty}^2}\right] \qquad = -\frac{2u}{U_{\infty}}$$
 (8)

In the above,  $U_{\infty} = 1$ , the normalized freestream speed, a =local speed of sound, M =local Mach number, V = the total velocity, p =local static pressure,  $P_{0} = \text{stagnation pressure}$ , and  $C_{p} = \text{pressure coefficient}$ .

# 3. NUMERICAL SOLUTION PROCEDURES

The concept of finite elements in conjunction with the method of weighted residuals (MWR) is the basis of the present numerical procedures in solving the small perturbation transonic flow equation. Of all the MWR methods, the Galerkin and the least squares approaches were investigated (Chan et al., Ref. 1), of which only the latter approach was found applicable to mixed flow analyses. The success with the least squares formulation is attributable to the resulting matrix being positive definite and well conditioned. This approach was therefore incorporated in the present computer program, with numerical procedures described in the following subsections. These include the finite element formulation, element description, special considerations in the supersonic region, the imposition of boundary conditions and iterative procedures.

# 3.1 Finite Element Formulation

The finite element method, in conjunction with the least squees method of weighted residuals, is used herein to solve numerically the small perturbation transonic equation. In this approach, a set of locally defined trial functions with undetermined parameters is assumed as the approximate solution, and the integral expression for the square of errors committed by the approximate solution is formulated. Then the integral of square errors in the entire domain is minimized with respect to the undetermined parameters to yield a system of algebraic equations. In actual computations, the minimization process is performed at element level and then an assembling process is invoked to obtain the system of algebraic equations. It is these processes which enable us to take care of the supersonic pocket with convenience and success. This special assembly technique is described in Section 3.3.

Written in the usual manner with repeated indices implying summation, the approximate solution has the following form

$$\widehat{\phi} = N_i \phi_i \tag{9}$$

in which  $N_i$ 's represent the shape functions and  $\phi_i$ 's are the undetermined parameters at nodal points. The residual then becomes

$$R = \left\{ \left[ 1 - M_{\infty}^2 - M_{\infty}^2 (1 + \gamma) N_{k,x} \phi_k \right] N_{j,xx} + N_{j,yy} \right\} \phi_j \quad (10)$$

from which an integral expression for the square errors is obtained as

$$\chi = \iint \mathbb{R}^2 dA \tag{11}$$

Upon the minimization of  $\chi$  with respect to the undetermined parameters, a system of algebraic equations in the following form is obtained

$$S_{ij} \phi_{j} = 0 \tag{12}$$

Herein the banded system matrix S<sub>ij</sub> is defined as

$$S_{ij} = \iint P_i Q_j dA \qquad (13)$$

with  $P_i$  and  $Q_j$  determined by the following expressions

$$Q_{j} = \left[1 - M_{\infty}^{2} - M_{\infty}^{2} (1 + \gamma) N_{k,x} \phi_{k}\right] N_{j,xx} + N_{j,yy}$$
 (14)

and

$$P_{i} = Q_{i} - M_{\infty}^{2} (1 + \gamma) N_{k,xx} \phi_{k} N_{i,x}$$
(15)

As stated earlier, the system matrix is obtained by combining appropriate contributions from all the elements. The element matrices, in turn, are evaluated effectively by numerical integration to avoid the tedious and error prone algebraic manipulations. The one presently used is a 7 point Gaussian quadrature, which can integrate exactly a quintic polynomial in the element. It is to be noted that although the system of equations, Equation (12), is homogeneous; it does possess a non-trivial solution once the boundary condition on the airfoil is imposed.

# 3.2 Element Description

The basic element used in the present program is the nonconforming cubic triangular element developed by Bazeley et al. (Ref. 2). Also used in the program are quadrilateral and trapezoidal elements constructed from these triangular elements. These three types of elements can be mixed and used freely in the entire flow region except that only trapezoids should be used to cover adequately the supersonic region in order to enact the special treatment discussed later.

The basic triangular element is shown in Fig. 2, which at each vertex has the function itself and its two first derivatives (velocity components) as undetermined parameters. This type of element was adapted mainly because boundary conditions of both Dirichlet and Neumann types can be imposed with

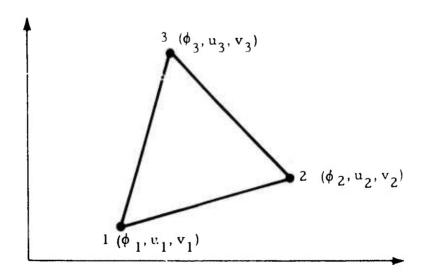


Figure 2 - Triangular Element with Undetermined Parameters

equal convenience. In addition, because velocities at nodes are treated as primary unknowns, secondary unknowns such as local Mach number, and pressure coefficients, etc. can be computed directly without resorting to numerical differentiation and thus assuring higher accuracy. Furthermore, the use of higher order elements can usually improve computational efficiency as evidenced in most finite element analyses.

In the element, the approximate solution is assumed as

$$\phi^e = N_i \phi_i \quad (i = 1 \text{ to } 9)$$

in which  $\phi_i$ 's are the nine undetermined parameters of  $\phi$  and its first derivatives at the nodal points as shown in the figure and  $N_i$ 's are the corresponding shape functions, which are expressed in terms of area coordinates.

Defined in the following are these shape functions and their first and second derivatives.

Letting

$$a_{i} = x_{j}y_{k} - x_{k}y_{j}$$

$$b_{i} = y_{j} - y_{k}$$

$$c_{i} = x_{k} - x_{j}$$

$$\Delta = \text{area of triangle } 1-2-3 = (b_{j}c_{k} - b_{k}c_{j})/2$$

$$\alpha = 0.5 (c_{k}-c_{j})$$

$$\beta = 0.5 (b_{j}-b_{k})$$

$$H = \zeta_{i}\zeta_{j}\zeta_{k}$$

$$H_{x} = b_{i}\zeta_{j}\zeta_{k} + b_{j}\zeta_{k}\zeta_{i} + b_{k}\zeta_{i}\zeta_{j}$$

$$H_{y} = c_{i}\zeta_{j}\zeta_{k} + c_{j}\zeta_{k}\zeta_{i} + c_{k}\zeta_{i}\zeta_{j}$$

$$H_{xx} = 2(\zeta_{i}b_{j}b_{k} + \zeta_{j}b_{k}b_{i} + \zeta_{k}b_{i}b_{j})$$

$$H_{yy} = 2(\zeta_{i}c_{j}c_{k} + \zeta_{j}c_{k}c_{i} + \zeta_{k}c_{i}c_{j})$$

with i=(1,2,3), j=(2,3,1), k=(3,1,2), then one has for  $\ell=(1,4,7)$ , i=(1,2,3),

$$N_{\ell, x} = \zeta_{i}^{2} (3-2\zeta_{i}) + 2H$$

$$N_{\ell, x} = \frac{1}{2\Delta} \left[ 6b_{i}\zeta_{i}(1-\zeta_{i}) + 2H_{x} \right]$$

$$N_{\ell, y} = \frac{1}{2\Delta} \left[ 6c_{i}\zeta_{i}(1-\zeta_{i}) + 2H_{y} \right]$$

$$N_{\ell, xx} = \frac{1}{(2\Delta)^{2}} \left[ 6b_{i}^{2}(1-2\zeta_{i}) + 2H_{xx} \right]$$

$$N_{\ell, yy} = \frac{1}{(2\Delta)^{2}} \left[ 6c_{i}^{2}(1-2\zeta_{i}) + 2H_{yy} \right]$$

for l=(2,5,8), i=(1,2,3)

$$N_{\ell} = \zeta_{i}^{2}(c_{k}\zeta_{j}-c_{j}\zeta_{k}) + \alpha H$$

$$N_{\ell,x} = \frac{1}{2\Delta} \left[ 2b_{i}\zeta_{i}(c_{k}\zeta_{j}-c_{j}\zeta_{k}) + 2\Delta\zeta_{i}^{2} + \alpha H_{x} \right]$$

$$N_{\ell,y} = \frac{1}{2\Delta} \left[ 2c_{i}\zeta_{i}(c_{k}\zeta_{j}-c_{j}\zeta_{k}) + \alpha H_{y} \right]$$

$$N_{\ell,xx} = \frac{1}{(2\Delta)^{2}} \left[ 2b_{i}^{2}(c_{k}\zeta_{j}-c_{j}\zeta_{k}) + 4b_{i}(2\Delta)\zeta_{i} + \alpha H_{xx} \right]$$

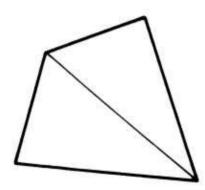
$$N_{\ell,xx} = \frac{1}{(2\Delta)^{2}} \left[ 2c_{i}^{2}(c_{k}\zeta_{j}-c_{j}\zeta_{k}) + \alpha H_{yy} \right]$$

for l=(3,6,9), i=(1,2,3)

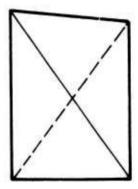
$$\begin{split} N_{\ell} &= \zeta_{i}^{2}(b_{j}\zeta_{k} - b_{k}\zeta_{j}) + \beta H \\ N_{\ell,x} &= \frac{1}{2\Delta} \left[ 2b_{i}\zeta_{i}(b_{j}\zeta_{k} - b_{k}\zeta_{j}) + \beta H_{x} \right] \\ N_{\ell,y} &= \frac{1}{2\Delta} \left[ 2c_{i}\zeta_{i}(b_{j}\zeta_{k} - b_{k}\zeta_{j}) + 2\Delta\zeta_{i}^{2} + \beta H_{y} \right] \\ N_{\ell,y} &= \frac{1}{(2\Delta)^{2}} \left[ 2b_{i}^{2}(b_{j}\zeta_{k} - b_{k}\zeta_{j}) + \beta H_{xx} \right] \\ N_{\ell,yy} &= \frac{1}{(2\Delta)^{2}} \left[ 2c_{i}^{2}(b_{j}\zeta_{k} - b_{k}\zeta_{j}) + 4c_{i}(2\Delta)\zeta_{i} + \beta H_{yy} \right] \end{split}$$

The undetermined parameters are arranged in the order of  $\phi_1$ ,  $u_1$ ,  $v_1$ ,  $\phi_2$ ,  $u_2$ ,  $v_2$ ,  $\phi_3$ ,  $u_3$ , and  $v_3$ .

Quadrilateral and trapezoidal elements as shown in Fig. 3 are also used in the present program, the former in purely subsonic flow region to save data input and the latter in the mixed and supersonic flow region. The element matrix for a quadrilateral is obtained by combining appropriately the matrices for two triangles, while matrix for a trapezoidal element is



a. Quadrilateral Element



b. Trapezoidal Element

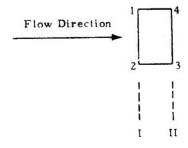
Figure 3 - Elements Constructed from Basic Triangles

obtained by combining and averaging contributions from four triangles, two left-running and two right-running triangles. The averaging process is designed to remove the bias effects inherent in the quadrilaterals presently used. In any event, the present program is coded in such a way that the computer is given the jurisdiction over which type of element to use, according to the flow behavior in the element. Of course, it does no harm to use trapezoids where the usage of quadrilaterals is considered adequate, except that computation time will increase slightly.

# 3.3 Special Considerations for Supersonic Region

As is well known, the finite element method is a powerful tool for solving problems governed by elliptic equations. However, for problems governed by either parabolic or hyperbolic equations, the conventional finite element assembly technique must be modified so that the proper influence of solution in time (or time-like direction) is considered. For the present problem, the x-axis is a time-like direction which implies that the solution at the upwind station will determine the solution at its downwind station but not the contrary. This consideration leads to the well known upwind influence finite difference operator (backward finite difference). An equivalent technique in finite element analysis has been devised and applied to solve the transonic flow equation.

Consider the rectangular element sketched below with upwind station I and downwind station II, each having two nodal points. With the element type chosen, the element matrices can be constructed in the usual manner. However, before assembling the element matrices into the system matrix, the coefficient of the



first term in the transonic equation should be evaluated

$$C = 1 - M_{\infty}^2 - M_{\infty}^2 (1 + \gamma) u$$
 (16)

The sign of the coefficient C being positive, zero, or negative will define the equation as elliptic, parabolic or hyperbolic. If C is non-positive for all nodes in the element, the rows representing the improper downwind influence on solution at an upwind station are ignored during assembly. This feature is taken care of automatically in the program, requiring only a little care with the nodal arrangement in the element. In the anticipated supersonic region, element node points should be arranged in the order as indicated in the above sketch, starting with the upper left corner node and proceeding in counterclockwise direction. On the other hand, if the sign of C is positive at any of the four nodes, no special assembling is invoked. As stated earlier, only trapezoidal elements are to be used in the anticipated supersonic and mixed flow region, while triangular elements and quadrilaterals consisting of only two triangles are considered unsuitable because of their bias nature. However, these two latter types of elements can be used effectively in the subsonic flow region.

# 3.4 Boundary Conditions and Iterative Procedures

As stated earlier, the imposition of boundary conditions for the present problem can be carried out conveniently because the elements presently used have function value and two first derivatives as primary unknowns. The associated boundary conditions thus can be treated as the essential type, i.e., having prescribed values. Standard finite element methodology is therefore followed by assembling first an unconstrained problem and then modifying the matrix equations accordingly. More specifically, on the outer boundary the flow is assumed to be undisturbed and hence the corresponding unknown parameters are set equal to zero. On the line of symmetry, the velocity component v is also set equal to zero. On the airfoil, the nonlinear form of flow tangency on the airfoil is imposed by replacing the algebraic equation for v by

$$\mathbf{v_i} - \frac{\mathrm{d}\mathbf{g}}{\mathrm{d}\mathbf{x}} \mathbf{u_i} = \frac{\mathrm{d}\mathbf{g}}{\mathrm{d}\mathbf{x}} \tag{17}$$

in which  $u_i$  and  $v_i$  are unknown parameters at node "i" on the airfoil. When the linear form is desired, the corresponding equation becomes

$$v_{i} = \frac{dg}{dx}$$
 (17a)

and is applied along the chordline. The selection between these two approaches is made through a control key in the input.

In the present program, no special efforts have been devoted to treat the leading edge and trailing edge singularities. Any rigorous approach should consider also the invalidity of small perturbation theory in these regions, which is certainly beyond the scope of the present study. Nevertheless, these regions are relatively small and the flow is usually subsonic in nature, which implies any error committed is generally localized and becomes less important elsewhere. For non-blunt airfoil such as a 6% thick circular arc, using half of the actual airfoil slope at each respective place in the computation seems to work well. However, for blunt airfoil such as NACA 64 A006, a finite slope near the leading edge, say 1% behind the airfoil leading edge, could be used in computing the vertical velocity component at that point. A still better approach is to use very fine elements in that region and treat the leading edge as a singular point. In practical computations, however, an element with its area approaching zero might create a new numerical problem because all shape function derivatives involve element area as divisor. Therefore, caution must be taken in using extremely small elements.

With the equations properly assembled and boundary conditions imposed, the system of nonlinear algebraic equations is finally solved by iterative procedures in the form

$$S_{ij}(\overline{\phi}) \phi_{j}^{(n)} = L_{i}$$
 (18)

to solve for the solution  $\phi^{(n)}$  at the n<sup>th</sup> iteration. The function  $\overline{\phi}$  is, in turn, defined as

$$\overline{\phi} = \theta \phi^{(n-1)} + (1-\theta) \overline{\phi}^{(n-1)}$$
 (19)

in which  $\theta$  is a relaxation factor in the range  $0 < \theta \le 1$ . For subsonic flows,  $\theta$  is usually taken as unity; for flow in the transonic regime, however, it has been found that the use of an under relaxation factor is required. The value of  $\theta$  should decrease from unity for barely critical flow to  $\theta$ . For even  $\theta$ , for supercritical flow. The optimum under-relaxation factor generally depends on the freestream Mach number and the mesh being used. At the present, no systematic investigations have been done in this regard, and therefore its value should be selected by numerical experimentations. Generally speaking, a smaller under-relaxation factor will make the solution more stable but at the same time tends to slow down the rate of convergence.

Equation (18) is to be solved subject to certain prescribed convergence criterion. The one presently used is that the relative change of local Mach number between two consecutive iterations should be less than a prescribed small number for all the nodes in the flow field, that is

$$\left| \frac{M^{(n)} - M^{(n-1)}}{M^{(n)}} \right| < \epsilon \tag{20}$$

Numerical experimentations indicate that a solution with adequate accuracy is generally obtainable with  $\epsilon$  in the range  $0.01 \le \epsilon \le 0.001$ .

### 4. PROGRAM DESCRIPTIONS AND USAGE

As stated earlier, the present computer program is capable of analyzing steady transonic flow over nonlifting thin airfoils by solving the small disturbance but nonlinear transonic potential equation. The numerical algorithm is based on utilizing the finite element technique in conjunction with the least squares method of weighted residuals. To solve a particular transonic flow problem, an appropriate finite element mesh must first be set up, followed by using the numerical procedures summarized in Section 3. Thus the present programs are separated into two parts - the first part which generates the necessary mesh information from a limited number of input cards and the second part which carries out the analysis with element mesh generated in the first part. By doing so, the generated mesh can be fully inspected for its correctness prior to the analysis, and storage required in the second program can be accordingly determined to suit each particular problem. These two programs are designated STRANL-I and STRANL-II (Steady Transonic Flow by Lockheed, parts I and II, respectively) and are described in more detail in the following.

### 4.1 STRANL-I

### 4.1.1 Scope and Flow Chart

This program reads in a limited number of input cards and generates mesh information such as element nodes, nodal coordinates, boundary nodes and airfoil slope, etc., to be used in the second program. Additionally, the present program has two options — one for renumbering the nodes to yield a smaller bandwidth and the other to plot the generated mesh for quick inspection. A schematic flow chart of the program is shown in Fig. 4.

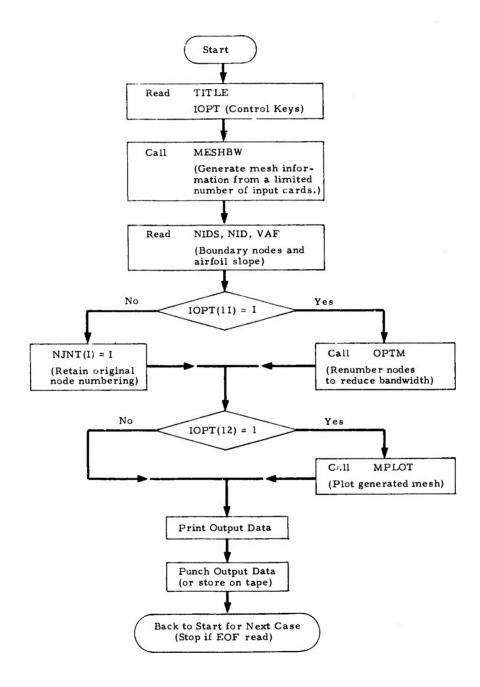


Figure 4 - Flow Chart of STRANL-I

The program as presently dimensioned requires approximately 428 words to run and can accommodate the following maxima:

- 200 elements
- 180 nodal points
- 50 nodes for each type of boundary conditions
- 10 nodes connected to any node in the mesh

# 4.1.2 Description of Variables

TITLE	Array used to describe the problem under consideration.
IOPT	Array containing the option keys which are activated when read in as "1." Presently there are two keys in the program, IOPT (11) for node renumbering option and IOPT (12) for mesh plot option.
NDEL	Array containing element node points.
X	Array containing the x-coordinate of nodal points.
Υ .	Array containing the y-coordinate of nodal points.
NJNT	Array containing the new nodal numbers if node renumbering option is executed; otherwise it retains the original nodal numbering.
MEMJT NEWJT JOINT JMEM	Arrays to provide adjustable dimensions used in subroutine OPTM for node renumbering.
NIDS	Array containing the actual number of boundary nodes for far field, on the line of symmetry, and along the airfoil surface.
NID	Array containing the nodal numbers for each type of boundary nodes mentioned above.
VAF	Array containing the airfoil slope for nodes on the airfoil surface.
NEM	Maximum number of elements allowed.
NPM	Maximum number of nodal points allowed.

NCN	Maximum number of nodes connected to any node in the mesh.
NEMN	Product of NPM with NCN.
NELS	Total actual number of elements.
NPS	Total actual number of nodal points.
MAXN	The maximum difference in nodal numbers between two connected nodes.
NBW	Full bandwidth of the resulting system matrix.

# 4.1.3 Subroutines

MESHBW: This subroutine is called to generate mesh information including the following: array of element nodes, total number of elements, x-and y-coordinates of nodal points, and the maximum difference in nodal numbers between two connected nodes. In generating this information, a small amount of input cards is required, which will be described under Section 4.1.4.

OPTM: This subroutine is called, when desired, to renumber the nodal points so as to yield as small a bandwidth as possible. The algorithm first establishes a table containing the nodal numbers connected to each of the nodal points, and then considers each node in turn as the origin of the new numbering system to search for one resulting in a smallest bandwidth. In consequence this subroutine generates an array of pointers relating the original numbering scheme to the new numbering scheme. This array is to be used in constructing the matrix equation, and is used again to refer back to the original numbering at output time. Using this method, one need not worry about the bandwidth problem and is unaware that any renumbering has taken place.

MPLOT: This routine plots the mesh generated together with the original node numbering, using the CALCOMP plotter. Correctness of the mesh can thus be checked quickly prior to running the second program.

# 4.1.4 Input and Output

All input and output are referred to the original numbering scheme, with input in the form of punch cards, and output in the form of printout and punch cards. If subroutine MPLOT is called, the mesh is also plotted for the convenience of inspection.

# Input

Input cards to this program should be prepared and provided in the order described below.

- A. TITLE CARD (7A10, A2)
  - Col. 1-72 Description of the problem under study
- B. OPTIONS CARD (4012)
  - Col. 22 Punch "l" if node renumbering is desired Col. 24 Punch "l" if mesh plot is desired
- C. ELEMENT CARDS (1615)

These are cards supplied to generate element nodal numbers in groups. One card is needed for each group of elements whose nodes are related in a regular pattern. The number of elements in a group can vary from one to any positive integer number, depending on how the nodes are numbered originally. There can be as many cards as required to generate the element nodes, and a blank card is added at the end to terminate the process.

Col.	Description
1-5	Number of nodes per element. Punch 3 for triangular elements, and punch 4 for quadri lateral and trapezoidal elements.
6-10	Number of elements in one direction (called first direction).
11-15	Number of elements in the other direction (called second direction).
16-20	Increment of nodal numbers in the first direction.
21-25	Increment of nodal numbers in the second direction.

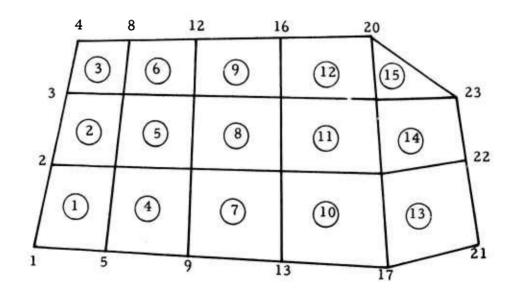
26 - 30	First nodal number in the element
31-35	Second nodal number in the element
36 - 40	Third nodal number in the element
41 - 45	Fourth nodal number in the element ("0" for triangles)

As stated before, element nodes are presently ordered in the counterclock-wise direction, and the upper left corner node should be taken as the first nodal point in an element located in the anticipated supersonic region. This is required to enact the assembling process correctly in the supersonic pocket.

For example, to generate element nodes for a mesh shown below, three input cards are required: one card for the first 12 elements, second card for the next two elements, and the third card for the triangular element. The three cards are:

4	4	3	4	1	2	1	5	6
4	1	2	0	1	18	17	21	22
3	1	1	0	0	20	19	23	0

(Ended by a blank card when all elements are covered)

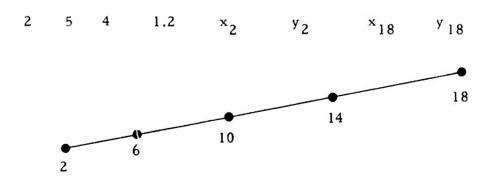


- D. CARD FOR TOTAL NO. OF NODES (15)
  - Col. 1-5 Total number of nodes for the entire flow region.
- E. NODE COORDINATE CARDS (315, 5F10.0)

The x- and y-coordinates of nodes are also generated in connected groups. A connected group of nodes are those falling on a straight line with a constant ratio of nodal distances and constant increment in nodal numbers as well. The intermediate nodal points can thus be generated by linear interpolation. Again, the process is terminated by encountering a blank card.

Col.	Description
1-5	Node number of the beginning nodal point.
6-10	Total number of nodes on the line.
11-15	Increment of nodal numbers between two consecutive nodes.
16-25	Ratio of distances between three consecutive nodes.
26-35	x-coordinate of the beginning node.
36-45	y-coordinate of the beginning node.
46 - 55	x-coordinate of the end node.
56-65	y-coordinate of the end node.

For example, to generate the coordinates for the nodes depicted below with a constant distance ratio of 1.2, the input card should read as



# F. CARD FOR NO. OF NODES ON BOUNDARIES (1615)

Col.	Description				
1 -5	Number of nodes on the outer boundary (called NFARF)				
6-10	Number of nodes on line of symmetry (called NWAKE)				
11-15	Number of nodes on the airfoil surface (called NBODY)				

# G. CARDS FOR BOUNDARY NODES (1615)

- (a) Nodes on the outer boundary (NFARF entries)
- (b) Nodes on line of symmetry (NWAKE entries)
- (c) Nodes on the airfoil surface (NBODY entries)
- H. CARDS FOR SLOPE ON AIRFOIL (8F10.0)

  Airfoil slope for nodes on the airfoil surface (NBODY entries)

# Output

The output from this program is in the form of printout, punch cards, and also a plot if the mesh plot option is invoked.

The following items are printed in the order as described:

- Title of the problem under study
- Control keys specified in the options card
- Total number of elements, number of nodal points, and the full bandwidth
- Element numbers and element node points
- Nodal numbers and their corresponding x- and y-coordinates
- Nodes on each type of boundaries
- Slope for nodes on the airfoil surface

The above items except the first two, together with the NJNT array relating the new node numbering to the original node numbering, are then punched and saved as input to the second program (STRANL-II).

# 4.2 STRANL-II

# 4.2.1 Scope and Flow Chart

This program carries out the analysis following the numerical procedures described in Section 3, with any mesh information generated and supplied through the first program. In summary this program solves the small perturbation transonic potential equation via the least squares finite element technique. The embedded supersonic pocket is taken care of by a proper assembling scheme and the resulting system of nonlinear algebraic equations is solved by direct iterative scheme. The present program has three options, one for inputting nonzero initial guess of the solution, one for computing in the same run solutions for higher Mach number(s) using results computed for lower Mach number case(s), and the last one for selecting the form of boundary condition on the airfoil. A schematic flow chart of the program is shown in Fig. 5.

The program as presently dimensioned requires approximately 1608 K words for the program itself and can accommodate the following maxima:

- 200 elements
- 180 nodal points
- 50 nodes for each type of boundary conditions
- 84 in full bandwidth of the resulting matrix equations

### 4.2.2 Description of Variables

IOPT

TITLE Array used to describe the problem under consideration

Array containing the option keys which are activated when read in as "1." Presently there are three options: IOPT(1) for continuation for high Mach number cases while using existing results computed for lower Mach number, IOPT(2) for inputting non-zero initial guess (referred to the new numbering system), and IOPT(3) for selecting the linearized boundary condition applied along the airfoil chordline.

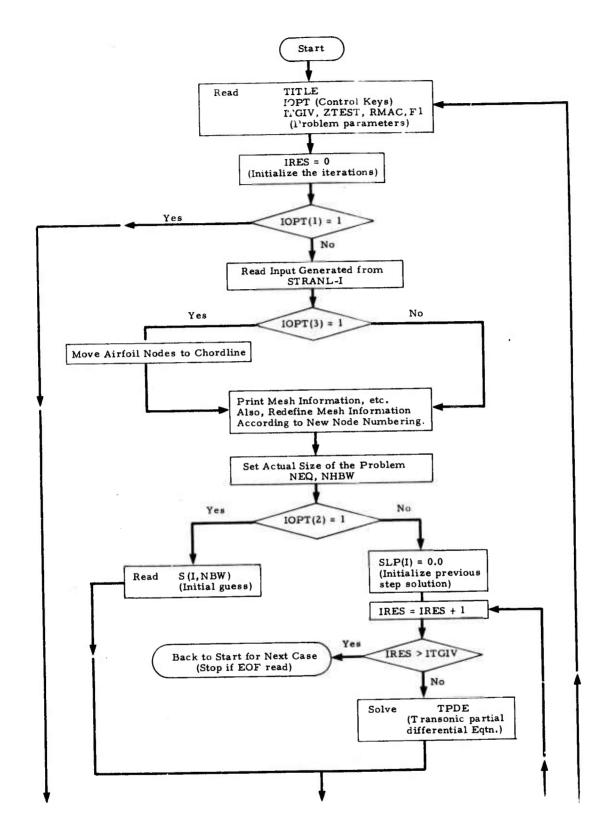


Figure 5 - Flow Chart of STRANL-II

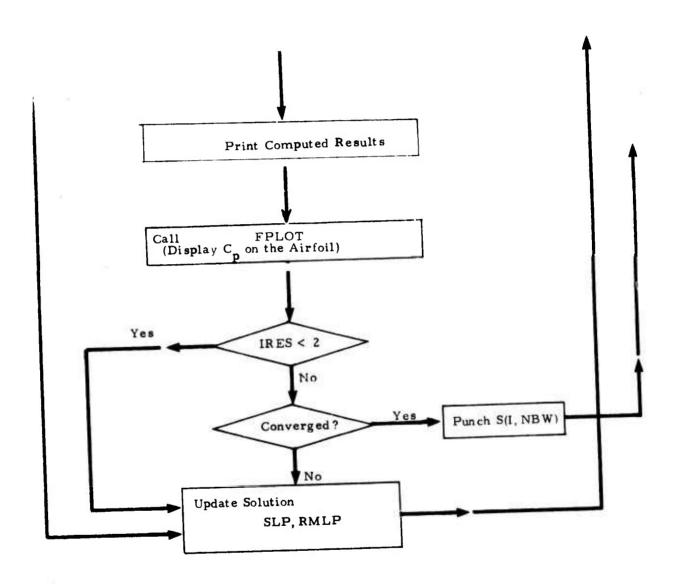


Figure 5 - (Concluded)

NOD	Array containing element node points
S	The resulting system matrix with main diagonal terms stored in the column numbered NHBW. After solving, the column numbered NBW contains the solution.
SLP	Array containing the solution obtained from rexalation procedures. This solution is used in generating the system matrix to solve for the next iterative solution.
X	Array containing the x-coordinate of nodal points.
Y	Array containing the y-coordinate of nodal points.
RML	Array containing values of local Mach number at nodal points for the current iteration.
RMLP	Array containing values of local Mach number at nodal points for the previous iteration.
COF	Array containing values of $M_{\infty}^2 + M_{\infty}^2$
	$(1 + \gamma)$ u evaluated at nodal points.
NJNT	Array relating the new node number- ing to the original node numbering schemes.
NIDS .	Array containing the actual number of boundary nodes for far field, on the line of symmetry, and along the airfoil, respectively.
NID	Array containing the nodal numbers for each type of boundary nodes mentioned above.
VAF	Array containing the airfoil slope for nodes on the airfoil surface.
AR	Array to store values for use in sub- routine FPLOT.
LR	Another array to be used in the sub- routine FPLOT.
NEM	Maximum number of elements allowed.
NPM	Maximum number of nodal points allowed.

NCM	Maximum full bandwidth allowed in the resulting system matrix.
NA	Maximum number of nodes allowed on the airfoil surface.
NRM	Maximum number of equations allowed.
NELS	Total actual number of elements.
NPS	Total actual number of nodal points.
NBW	Full bandwidth of the resulting system matrix.
NHBW	Half bandwidth of the resulting system matrix.
NEQ	Number of equations in the resulting system of equations.
ITGIV	Cut-off number of iterations.
ZTEST	Small number used to check convergence based on the relative change of local Mach number between two consecutive iterations.
RMAC	Freestream Mach number.
SQMAC	Square of the freestream Mach number.
Fl	Under-relaxation factor with $0 < F1 \le 1.0$ .
IRES	Number of iterations.
POT	Perturbed velocity potential.
UPT	Perturbed velocity component in the x-direction.
V	Perturbed velocity component in the y-direction.
U	Total velocity component in the x-direction.
PRATIO	The ratio of local static pressure to stag- nation pressure.
CP	Pressure coefficient.
DELM	Change of local Mach number between two consecutive iterations.

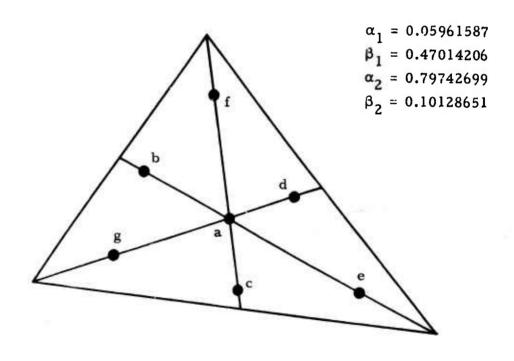
## 4.2.3 Subroutines

NEWK: This subroutine is called in the main program to generate system matrix for the entire flow field by assembling appropriately the element

matrices. The elements are, in general, a combination of triangles, quadrilaterals and trapezoids. For a 4-node element, this subroutine also determines either to treat it as a quadrilateral or as a trapezoid, depending on the local behavior of the governing equation being elliptic or otherwise. Subroutine EMQT is called to generate the element matrices.

EMQT: This subroutine generates element matrix for elements in the form of triangles, quadrilaterals and trapezoids. Element matrix for the later two types is obtained by combining appropriately (and averaging for the last type) contributions from triangular elements which are in turn evaluated in subroutine EMTC.

EMTC: This subroutine evaluates the element matrix for a triangular element by numerical integration. The one presently used is a 7-point Gaussian quadrature, which can integrate exactly a quintic polynomial in the element. Shown below are the locations of these Gaussian points with their corresponding weights shown on page 31.



Points	Area	Coord	dinates	Weights
a	1/3	1/3	1/3	0.225
b	αι	$\beta_1$	β	
С	β	$\alpha_1$	$\beta_1$	0.13239415
d	β	$\beta_1$	$\alpha_1$	
е	α2	$\beta_2$	$\beta_2$	
f	β <sub>2</sub>	$\alpha_2$	$\beta_2$	0.12593918
g	β2	β <sub>2</sub>	α <sub>2</sub>	

<u>DERV</u>: This is a subroutine called by EMTC to evaluate the first and second derivatives of the shape functions at a Gaussian point, based on the expressions listed in Section 3.2.

BNDEQ: This is an equation solver for banded nonsymmetric system of algebraic equations, utilizing the direct Gaussian elimination scheme. In this solver the system matrix is arranged in a twisted form such that main diagonal terms are stored in the column numbered NHBW and the right-hand side vector is in the column NBW. After solving, the column numbered NBW contains the solution vector.

<u>FPLOT</u>: FPLOT collects and stores data as it becomes available, and upon signal, produces a printer plot in practically any orientation and size. It should be regarded as a general purpose output routine for displaying output data in graphical form.

### Description of Parameters

Ml	Size of the main storage array, and it should never be larger than 800, which corresponds to 400 points to be plotted.
IPNT	Counter initialized — usually IPNT = 0 - in the calling program. It is incremented by 2 each time a new data point is entered in AR.

	dimension statement in the calling pro- gram. For example, DIMENSION AR(800).
LR	An array of bytes used to hold the curve number. It should be dimensioned for M1/2. The type declaration LOGICAL*1 LR(400) should be in the calling program.
ISTOP	Flag used to signal that all data has been entered. ISTOP = 0 causes data to be stored. If ISTOP = -1 and NC = NCMAX the program immediately branches to the plotting section. If ISTOP = 1 and NC = NCMAX a data point is stored and then the

Main storage array. It should be in a

NC Curve number for which data is being entered. It must be a positive integer less than 21.

plotting section is entered.

NCMAX The number of curves to appear on the graph.
This is the largest value NC will have.

V1 The horizontal coordinate of the data point to be plotted.

V2 The vertical coordinate of the data point to be plotted.

#### 4.2.4 Input and Output

AR

## Input

The bulk of input to this program is provided through STRANL-I in the form of punch cards. To run several cases of various freestream Mach number but using the same mesh and boundary conditions, three additional cards should be furnished for each case to be computed. These cards should be provided in the following order

A. TITLE CARD (7A10, A2)

Col. 1-72 Description of the problem under study

- B. OPTIONS CARD (4012)
  - Col. 2 Punch "1" if it is a continuation in computation from one Mach number to another.

Col. 4 Punch "!" if cards for nonzero initial guess is furnished in the input data. If so, insert them following those generated from STRANL-I.

Col. 6 Punch "l" if linearized boundary condition along the chordline is desired.

NOTE: As seen in the flow chart, when IOPT(1) = 1, the last two options become inoperative.

## C. PROBLEM PARAMETERS CARD (I5, 3F10.0)

Col. 1-5 Cut-off number of iterations.

Col. 6-15 Small number used to check convergence based on the relative change of local Mach number between two consecutive iterations, usually taken in the range from 0.01 to 0.001.

Col. 16-25 Freestream Mach number

Col. 26-35 Under relaxation factor with the value of 1.0 for subsonic cases, and decreasing for supercritical flows.

For the first case of the run, punch cards from STRANL-I are placed after the above cards. For subsequent cases using the same mesh, three additional cards as described above are required for each case.

#### Output

The output from this program include printout, referred to the original numbering system, and punch cards as well for the cases whose solutions are convergent.

The printouts are in the following order:

- Title of the problem under study
- Convergent limit

- · Control keys specified in the options card
- Total number of element, number of nodal points, and the full bandwidth of the resulting matrix equations
- Element numbers and element node points
- Nodal numbers and their corresponding x- and ycoordinates
- Boundary nodes for each type of boundaries
- Slope for nodes on the airfoil surface
- For each iteration, the computed results at all nodal points are printed. These include the perturbed velocity potential, total velocity components in the x- and y-directions, the value of  $M_{\infty}^2$  (1 + 2.4 u), local Mach number, the ratio of local static pressure to stagnation pressure coefficient, and finally the change of local Mach number between two consecutive iterations.
- For each iteration, the value of C<sub>p</sub> along the airfoil is displayed graphically.

#### 5. SAMPLE CASES

Two sample cases are presented herein to demonstrate the usage of the computer programs described in the previous section regarding input and typical output from the programs. The two problems are flow over a NACA 64 A006 airfoil analyzed with a coarser mesh and flow over a 6% thick circular arc computed with a finer mesh where the nodes are renumbered to reduce the bandwidth.

In computing a transonic flow field for a given airfoil shape with the present programs, the following procedures are generally followed:

- A desired mesh is sketched with each node assigned a number.
- Based on the mesh sketched, an appropriate set of input cards is prepared and supplied to STRANL-I to generate the required mesh information in the form of punch cards.
- The above punch cards, with three additional cards for each case and cards for non-zero initial guess if available, are used as input to STRANL-II to compute the flow field.
- During the execution of STRANL-II, results for each iteration are printed, and for solution satisfying convergent criterion the solution is saved in the form of punch cards for possible later use.

The following paragraphs describe in more detail the input and output for the two sample problems.

# 5.1 Flow Over a 6% Thick Circular Arc Airfoil

This problem was analyzed using the mesh shown in Sketch 1 which consists of 154 elements together with 170 nodes. Note that a relatively regular mesh is adapted in the anticipated supersonic region while the

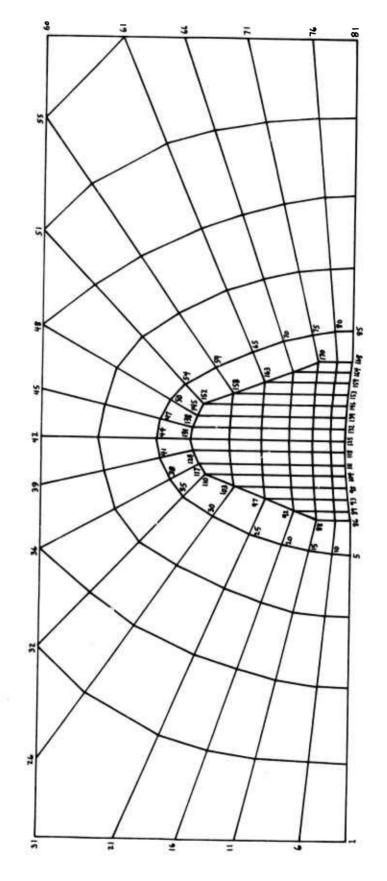


Figure 6 - Freehand Sketch of Finite Element Mesh for 6% Thick Circular Arc Airfoil

remaining elements are arranged rather arbitrarily. Also, the nodal points need only be numbered according to convenience, as the node renumbering option will be invoked to renumber them to yield a smallest bandwidth. With the present mesh, although a little more effort is required in preparing input cards to the STRANL-I program, the elements are considered to have been used more effectively than a regular mesh. Summarized below are the input and output to the STRANL-I and STRANL-II programs for the present problem.

## 5.1.1 STRANL-I

## Input

The necessary set of input cards is listed on the next three pages. Note that both options for plotting mesh and node renumbering are to be enacted, and the final mesh will have nodes on the actual airfoil surface rather than on the chordline.

INPUT CARDS TO STRANL-1 FOR CIRCULAR ARC AIRFOIL

STEADY TRANSONIC FLUW--MESH 6--154 ELEMENTS.170 NODES

5 2 8 8	4 6
75 80 85 89 92	93 97 98 103
7 9 9 9 9	89 96 93 102
167 170 169 87 88	90 92 94 94
00000	0000
00040	0-0-
	n - 4 -
4444	4 11 4 11
	1 0 0 167 170 75 1 0 0 170 169 80 1 0 0 169 168 85 1 1 0 87 86 89 1 0 0 88 91 92

													•	•	•	0.43	•		0.86	1.08	1.15	1.22	1.25	N	1.15	1.06	0.86		Ŏ	4	Ñ	-	0	N	3	ហ		0.92	
													1.80	1.81	1.82	1.86	1.92		0	7	8	63	ល	9	2.75	8	5		0		• 1	•2	2	0	0	•	•20	2.275	6.3
105		112	S		160		165		169				0	0	0	0	0	0	0	0	o	ō	ō	ō	o	0	00	0	0	0	0	0	0	0	57	31	192	2	273
0	110	111	S	158	S	163	164	167	168	170																	2.0		1.5	•	•	0.3	•	•	0.0	•	0.0	•	0
86	109	104	4	រូ	153	157	159	162	164	166			_	_	•	_	_	_	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	'n	25	0	75	ເດ
66	103	105	147	152	154	158	160	163	165				0	0.0	0.00	0.00	0.00	0.00	0.5	1.2(	1.8(	2.2	2.5	2.8(	3.2	3.8(	4.50	5.0	5.0	5.0	5.0	5.0	500	2.00	2.0	2.1	2.2	2.2	2.3
0	0	7	0	0	0	0	0	0	0	0																													
-4	0	7	-4	0	~	၁	7	0	<b>-</b>	0			16	91	16	Φ	83	0	91	16.	87	87	.91	.87	.87	.91	0.910	0	.83	87	91	5	.91	2	7	. 4		. 7	1.20
1	7	9	p=4	-	-	-	-		-	-	(p.		7	1	7	-	-	0	-	-	-	-	~	-	-	-	1	0	-	-	-	-	-	-	-	-	-		
ß	~	9	រហ	-	4	-	ო		7	1	blank card		ഗ	ഗ	ហ	ហ	ហ	-	ស	4	n	n	m	n	n	4	ഗ		ທ	ហ	រ	ល	ហ	n	4	ഗ	0	7	7
₹	က	4	4	m	4	n	4	n	4	'n	(bla	170	-	9	11	16	21	31	56	32	36	39	42	45	48	5.1	52	9	19	99	7.1	76	81	90	68	93	96	104	

										9				000	
								-		22			168	+0000	
										21			164	194	5022
										48			159	+0.01	-0.06022
1.02	1.00	96.0	0.92	0.75	0.55	0.35	0.22			45			153	5858	9850
_	ঠ		ហ្វ		ស		_			42			146	+0.0	-0.10620
2.50	2.5	2.65	2.72	2.80	2.87	2.95	3.00			39			139	5385	9004
3000	5933	:731	2394	1922	1315	572	_			36			132	+0.0	-0.09004
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0			35		82	125	7193	7193
•	ī.	·O	52	_	75	10	•			31		84	118	+000	-0.07193
2.50	2.5	2.6	2.72	2.80	2.8	2.9	3.00			56		83	111	9004	5388
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125	132	139	146	153	159	164	168	(bla	21	-	61	N	90	•06	•01
	0.03000	2.50 0.03000 2.50 2.575 0.02933 2.575	2.50 0.03000 2.50 2.575 0.02933 2.575 2.65 0.02731 2.65	7 1 1.20 2.50 0.03000 2.50 7 1 1.20 2.575 0.02933 2.575 7 1 1.20 2.65 0.02731 2.65 7 1 1.20 2.725 0.02394 2.725	7 1 1.20 2.50 0.03000 2.50 7 1 1.20 2.575 0.02933 2.575 7 1 1.20 2.725 0.02731 2.65 7 1 1.20 2.725 0.02394 2.725 6 1 1.20 2.80 0.01922 2.80	7 1 1.20 2.50 0.03000 2.50 7 1 1.20 2.575 0.02933 2.575 7 1 1.20 2.65 0.02731 2.65 7 1 1.20 2.80 0.01922 2.80 5 1 1.20 2.875 0.01315 2.875	7 1 1.20 2.50 0.03000 2.50 7 1 1.20 2.575 0.02933 2.575 7 1 1.20 2.65 0.02731 2.65 7 1 1.20 2.80 0.01922 2.80 5 1 1.20 2.875 0.01315 2.875 4 1 1.20 2.95 0.00572 2.95	7 1 1.20 2.50 0.03000 2.50 7 1 1.20 2.575 0.02933 2.575 7 1 1.20 2.65 0.02731 2.65 6 1 1.20 2.725 0.02394 2.725 6 1 1.20 2.80 0.01922 2.80 5 1 1.20 2.875 0.01315 2.875 4 1 1.20 2.95 0.00572 2.95 3 1 1.20 3.00 0.00	7 1 1.20 2.50 0.03000 2.50 7 1 1.20 2.575 0.02933 2.575 7 1 1.20 2.65 0.02731 2.65 6 1 1.20 2.80 0.01922 2.80 5 1 1.20 2.875 0.01315 2.875 4 1 1.20 2.875 0.01315 2.875 3 1 1.20 3.00 3.00	7 1 1.20 2.50 0.03000 2.50 7 1 1.20 2.575 0.02933 2.575 7 1 1.20 2.65 0.02731 2.65 7 1 1.20 2.725 0.02394 2.725 6 1 1.20 2.80 0.01922 2.80 5 1 1.20 2.875 0.01315 2.875 4 1 1.20 2.95 0.00572 2.95 8 15 8 15	7 1 1.20 2.50 0.03000 2.50 1.02 7 1 1.20 2.575 0.02933 2.575 1.00 7 1 1.20 2.65 0.02731 2.65 0.96 7 1 1.20 2.65 0.02731 2.65 0.96 7 1 1.20 2.80 0.02394 2.725 0.92 6 1 1.20 2.80 0.01922 2.80 0.75 5 1 1.20 2.875 0.01315 2.875 0.55 4 1 1.20 2.95 0.00572 2.95 0.35 3 1 1.20 3.00 0.00 3.00 0.22 llank card) 8 15 6 11 16 21 26 31 32 36 39 42 45 48 51 55	7 1 1.20 2.50 0.03000 2.50 1.02 7 1 1.20 2.575 0.02933 2.575 1.00 7 1 1.20 2.65 0.02731 2.65 0.96 7 1 1.20 2.65 0.02394 2.725 0.96 7 1 1.20 2.875 0.02394 2.725 0.95 5 1 1.20 2.875 0.01922 2.80 0.75 5 1 1.20 2.875 0.01315 2.875 0.55 4 1 1.20 2.95 0.00572 2.95 0.35 3 1 1.20 3.00 0.00 3.00 0.22 8 15 6 11 16 21 26 31 32 36 39 42 45 48 51 55 56 71 76 81	7 1 1.20 2.50 0.03000 2.50 1.02 7 1 1.20 2.575 0.02933 2.575 1.000 7 1 1.20 2.655 0.02731 2.655 0.96 7 1 1.20 2.65 0.002394 2.725 0.92 6 1 1.20 2.80 0.01922 2.80 0.075 5 1 1.20 2.875 0.01315 2.875 0.55 4 1 1.20 2.95 0.00572 2.95 0.35 3 1 1.20 3.00 0.00 3.00 0.22 lank card) 8 15 6 11 16 21 26 31 32 36 39 42 45 48 51 55 56 71 76 81 3 4 5 82 83 84 85	7 1 1.20 2.50 0.03000 2.50 1.02 7 1 1.20 2.575 0.02933 2.575 1.00 7 1 1.20 2.575 0.02933 2.575 1.00 7 1 1.20 2.65 0.02731 2.65 0.96 7 1 1.20 2.65 0.002394 2.725 0.92 6 1 1.20 2.80 0.01922 2.80 0.075 5 1 1.20 2.95 0.01315 2.875 0.55 4 1 1.20 2.95 0.00572 2.95 0.35 3 1 1.20 3.00 0.00 3.00 0.22 lank card) 8 15 6 11 16 21 26 31 32 36 39 42 45 48 51 55 56 71 76 81 3 4 5 82 83 84 85 3 9 93 98 104 111 118 125 132 139 146 153 159 164 168	7 1 1.20 2.50 0.03000 2.50 1.02 7 1 1.20 2.575 0.02933 2.575 1.00 7 1 1.20 2.575 0.02933 2.575 1.00 7 1 1.20 2.65 0.02731 2.65 0.096 7 1 1.20 2.65 0.02731 2.65 0.096 6 1 1.20 2.80 0.01922 2.80 0.075 5 1 1.20 2.875 0.01315 2.875 0.55 3 1 1.20 2.95 0.00572 2.95 0.35 3 1 1.20 3.00 0.00 3.00 0.22 lank card) 8 15 6 11 16 21 26 31 32 36 42 45 48 51 55 56 71 76 81 3 4 5 82 83 84 85 89 93 98 104 111 118 125 139 146 153 159 164 168 00022 +0.10820 +0.07193 +0.07193 +0.05389 +0.01794 +0.0000

## Output

As stated before, output of this program includes printouts, punch cards and a plot for the generated mesh.

Printouts and punch cards for the present mesh are listed on the next 12 pages.

## PRINT OUTS FROM STRAIN-I FOR CIRCULAR ARC AIRFOIL

STEADY TRANSONIC FLOW--MESH 6--154 ELEMENTS, 170 NODES

ELE. NO. AND ELEMENT NODES

1	31	21	26	8
2	6	1	2	7
3	11	6	7	12
4	16	11	12	17
5	21	16	17	22
6	26	21	22	27
7	7	2	3	8
8	12	7	8	1, 3
9	17	12	13	18
13	17 22	17	18	23
11	27	22	23	28
12	8	3	4	9
13	13	8	9	14
14	13	13	14	19
15	23	18	19	19
15 16 17 18	28	23	24	29
17	9	4	5	10
18	14	9	13	15
19	19	14	15	20
20	24	19	20	25
21	29	24	25	30
22	26	27 28	32	0
23	27	28	33	32
23 24 25	28	29	25 32 33 34	33
25	29	30	35	34
26	32	33	36	O

27	33	34	37	36
28	34	35	38	37
29	30	37	40	39
30	37	38	41	40
31	39	40	43	42
32	40	41	44	43
33	42	43	46	45
34	43	44	47	46
35	45	46	49	48
36	46	47	50	49
37	48	49	53	52
38	49	50	54	53
39	48	52	51	Đ
40	51	56	55	٠ ئ
41	51	52	57	56
42	52	53	58	57
43	53	54	59	58
44	<b>5</b> 5	61	60	8
45	55	56	62	61
46	56	57	53	62
47	57	58	64	63
48	58	59	65	64
49	61	62	67	06
50	62	63	68	67
51	63	64	69	58
52 53	64	65	70	69
73	66	67	72	71
54	67	68	73	12
55	68	69	74	73
56 57	69 71	76	75	74
53	72	72	77	76
59	73	73	78	77
60		74	79	78
61	74 76	75	80 82	79
62	77	77 78		81
63	78	79	83 84	82 33
64	79	80	85	84
65	1	- 5	86	87
66	15	10	87	88
67	21	15	88	32
63	25	20	92	97
69	30	25	97	133
70	35	30	103	110
71	38	35	110	117
72	41	38	117	124
73	44	41	124	131
74	44	131	138	47
75	47	138	145	50
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76	50	145	152	54
77	152	158	59	54
78	158	163	65	59
79	163	167	70	65
80	167	170	75	70
81	170	169	80	75
82	169	168	85	80
83	87	86	89	90
84	88	87	90	91
85	88	91	92	Ü
86	9 u	89	93	94
87	91	90	94	95
38	92	91	95	96
89	92	96	97	0
90	94	93	98	39
91	95	94	99	136
92	96	95	100	101
93	97	96	101	102
94	97	102	103	Ü
95	99	98	104	1.5
96	100	99	105	116
97	101	106	106	107
93	102	101	107	138
99	103	102	108	109
100	103	109	110	8
101	165	104	111	112
102	166	105	112	113
103	107	106	113	114
104	108	107	114	115
105	109	108	115	116
106	110	109	116	117
107	112	111	118	119
108	113	112	119	120
109	114	113	120	121
110	115	114	121	122
111	116	115	122	123
112	117	116	123	124
113	119	118	125	126
114	120	119	126	127
115	121	120	127	128
116	122	121	128	129
117	123	122	129	136
118	124	123	130	131
119	126	125	132	133
120	127	126	133	134
121	128	127	134	135
122	129	128	135	136
123	130	129	136	137
124	131	134	137	138
125	133	132	139	140

Landing the state of the state

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126
      134
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            162
                 157
152
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            164
                 158
                       169
153
      166
            165
                 159
                       170
154
      167
            166
                 170
```

OLD	NODE	NEW NODE	X(I)	Y(1)
	1	167	0.	0.
	2	168	.51551E+00	0.
	3	169	. 38453E+00	0.
	4	170	.14115E+#1	0.
	5	166	.1800JE+01	0.
	6	161	0.	.30000E+60
	7	162	.51838E+00	.24272E+00
	8	163	. 99010E+00	.19060E+00
	9	154	.14194E+01	·14316E+6J
	10	165	.18100E+01	.10000E+00
	11	153	0.	.70000E+G0
	12	154	.52124E+00	.57399E+00
	13	155	.39557E+00	.45931E+CJ
	14	156	.14272E+01	.35496E+00
	15	157	.1850 JE+01	.26000E+00
	16	144	0.	.11000E+01
	17	145	.56614E+00	.896G7E+GJ
	18	146	.10557E+01	.71865=+00
	19	147	:14872E+01	.56429E+00
	20	148	.18600E+01	.43000E+60
	21	134	0.	.15300E+G1
	22	135	.617+3E+00	·12299E+61
	23	136	•11324E+01	.10046E+01
	24	137	.15618E+01	.81670E+0J
	25	138	.19200E+01	.66000E+00
	2ó	122	.50000E+00	.20000E+C1
	27	123	·93532E+00	.16735£+G1
	28	124	.13315E+01	.13764E+01
	29	125	.1592JE+01	·11060E+61
	30	126	.20200E+01	.86000E+00
	31	133	0.	.20000E+G1
	32	111	.12000E+01	.20000E+G1
	33	112	.1535 JE+01	.16640E+C1
	34 35	113	.18418E+01	·13582E+01
	35 36	114	.21200E+01	•10800E+01
	36 37	101	.18000E+01	-20000E+G1
	37 30	102	.20496E+01	.15455E+01
	38	103	.22500E+01	• 11500E+01
	39	91	. 22000E+01	.20000E+01
	40	92	.22963E+01	,15829E+01

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.23800E+01
                                     .12200E+01
           93
41
                                     .20000E+01
42
           81
                   .25000E+01
                                     .16073E+91
           82
                   . 25000E+01
43
                   . 2500 UE+01
                                     .12500E+01
           83
44
                                     .20000E+01
           71
                    . 23000E+01
45
                                     .15829E+01
           72
                    .27037E+01
46
                    .26203E+01
                                     .12200E+01
47
           73
                                     .20000E+01
                    .3200UE+01
           61
48
                                     .15455E+01
                    .29534E+01
49
           62
                    .27500E+01
                                     .11500E+01
50
           63
                    .38000E+01
                                     .20000E+G1
           50
51
                                     .16567E+u1
           51
                    .34640E+01
52
                                     .13443E+01
53
            52
                    .31582E+01
54
            53
                    .28800E+01
                                     .106BOE+81
            38
                    .45000E+01
                                      .20000E+01
55
                                      .16735E+01
                    .40647E+01
            48
56
                                      .13764E+01
                    .36685E+01
57
            41
                                      .11060E+01
58
            42
                    .3308JE+01
                    .29800E+01
                                      .86000E+U0
59
            43
                                      .20000E+G1
            39
                    .50000E+01
60
                                      .15000E+01
                    .50000E+01
            28
61
                    .43826E+01
                                      .12299E+G1
            23
62
                                      .10046E+C1
63
            30
                    .38676E+01
            31
                    .34392E+01
                                      .81670E+GJ
64
                                      .66000E+00
65
            32
                    .30800E+01
                                      .11000E+01
                    .50000E+01
66
            16
                                      .90520E+C0
            17
67
                    .44278E+01
                    . 39299E+01
                                      .73572E+60
68
            19
                                      .58828E+03
            21
                    .34958E+01
69
                                      .46000E+G3
                    .31200E+01
70
            23
                                      .700G0E+00
            18
                    .5,000E+01
71
                                      .57339E+00
72
             7
                    .44782E+01
                                      .45931E+0J
                    .39890E+01
73
             8
 74
            10
                    .35493E+81
                                      .35496E+00
                    .31500E+31
                                      ,26000E+00
 75
            12
                    .50000E+01
                                      .30000E+00
            20
 76
             9
                                      . 24272E+00
 77
                    .44845E+01
             2
                     .46154E+01
                                      .19060E+00
 78
                                      .14316E+GD
 79
             3
                     .35885E+01
             5
                     .32000E+Q1
                                      .10000E+00
 80
                                     0.
            22
                     .50000E+81
 81
                     .44845E+01
                                     0.
 82
            11
                                     0 .
             4
                     .40154E+01
 83
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0.
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84
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                                     0.
             6
                    . 32000E+01
85
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                    . 20000E+01
86
           160
                                      .10000E+60
                    . 2U000E+01
           159
87
                    .20000E+01
                                      .22000E+00
           158
 88
                                      .57260E-G2
                    . 20500E+01
           152
 89
                                      .10030E+00
           151
                    .20500E+01
 90
                    .23503E+01
                                      .21380E+00
           150
 91
                    . 20500E+01
                                      . 35000E+C0
 92
           149
                                      .13150E-01
           143
                    .2125UE+01
 93
                     . 2125UE+01
                                      .11316E+00
           142
 94
                                      . 23317E+GD
                    .212505+01
 95
           141
                                      .37718E+00
                     .2125UE+01
           140
 96
                                      .55000E+03
                     .21250E+01
 97
           139
                     .22000E+01
                                      .19220E-01
 98
           132
                                      .11742E+00
                     . 22000E+01
 99
           131
                                      . 23526E+00
100
           130
                     . 22000E+U1
                     . 22000E+01
                                      .37668E+G0
           129
131
                                       .54637E+00
                     .22000E+01
           128
102
                                      .750COE+60
                     .22000E+01
           127
103
                                       .23940E-01
           121
                     .22750E+01
104
                                       .11418E+63
                     .22750E+01
           120
105
                                       .22246E+03
                     .22750E+01
           119
106
                                       .35241E+00
                     .2275UE+01
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107
                     .2275 JE+01
                                       .50834E+00
108
           117
                                       .69546E+00
                     . 22750E+01
109
           116
                                       .92000E+60
110
           115
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                     .23500E+01
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111
                                       .12124E+00
                     .2350 0E+01
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112
                                       .23395E+G0
            108
                     .23500E+01
113
                     .2350JE+01
                                       .36921E+00
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                                       .53151E+00
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116
                     .2350 0E+01
                                       .96000E+60
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            100
                                       .29330E-C1
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                                       .12708E+GD
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                     . 2425 UE+01
120
             97
                     .24250E+01
                                       .38515E+0J
121
                                       .55406E+G0
                     .2425 JE+01
             96
122
                                       .75676E+00
             95
                     .2425 DE+01
123
                                       .10000E+01
                     .2425 9E+91
124
             94
                     .25000E+01
                                       .30000E-01
125
             90
                                       .12978E+00
                      .25000E+01
126
             89
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127 88 .25000E+01 .24934E+08 128 87 .2500UE+01 .39290E+08 129 86 .25400E+01 .56518E+08 130 85 .25400E+01 .77192E+00 131 84 .25000E+01 .10200E+01 132 80 .25750E+01 .29330E-01 133 79 .2575UE+01 .2708E+01 134 78 .25750E+01 .24438E+00 135 77 .25750E+01 .38515E+00 136 76 .25750E+01 .55406E+00 137 75 .25750E+01 .75676E+00 138 74 .24750E+01 .10000E+01 139 70 .24750E+01 .10000E+01 140 69 .25500E+01 .27310E-01 140 69 .25500E+01 .23335E+00 141 68 .26500E+01 .35921E+00 142 67 .26500E+01 .53151E+00 144 65 .26500E+01 .72628E+00 145 64 .26500E+01 .72628E+00 146 60 .27250E+01 .33940E-01 147 59 .27250E+01 .35921E+00 148 58 .27250E+01 .35921E+00 148 58 .27250E+01 .35921E+00 150 55 .27250E+01 .35241E+00 151 55 .27250E+01 .35241E+00 152 54 .27250E+01 .35241E+00 153 49 .2300GE+01 .50834E+00 151 55 .27250E+01 .50834E+00 152 54 .27250E+01 .50834E+00 153 49 .2300GE+01 .59637E+00 154 48 .28000E+01 .37668E+G0 157 45 .2800JE+01 .3760E+01 160 36 .2875UE+01 .31150E-01 161 35 .2875UE+01 .33718E+C0 163 33 .28750E+01 .57200E-02 164 27 .29500E+01 .57200E-02 165 26 .29500E+01 .57200E-02 166 25 .29500E+01 .35000E+00 167 24 .29500E+01 .35000E+00 168 15 .30000E+01 .57200E-02 169 14 .3G00UE+01 .35000E+00				
129 86 .25000E+01 .77192E+00 130 85 .25000E+01 .77192E+00 131 84 .25000E+01 .10200E+01 132 80 .25750E+01 .29330E-01 133 79 .25750E+01 .12708E+01 134 78 .25750E+01 .24438E+00 135 77 .25750E+01 .38515E+00 136 76 .25750E+01 .75676E+01 137 75 .25750E+01 .75676E+00 138 74 .2750E+01 .75676E+00 139 70 .26500E+01 .27310E-01 140 69 .25500E+01 .27310E-01 140 69 .25500E+01 .23335E+00 141 68 .26500E+01 .36921E+00 144 65 .26500E+01 .55151E+00 144 65 .26500E+01 .76628E+00 145 64 .26500E+01 .76628E+00 146 60 .27250E+01 .35921E+00 147 59 .27250E+01 .23940E-01 147 59 .27250E+01 .22940E-01 148 58 .27250E+01 .35241E+00 149 57 .27250E+01 .35241E+00 150 56 .27250E+01 .35241E+00 151 55 .27250E+01 .35241E+00 152 54 .27250E+01 .50834E+00 153 49 .2300GE+01 .19220E-01 154 48 .28000E+01 .19220E-01 155 47 .28000E+01 .19220E-01 156 46 .28000E+01 .37668E+60 157 45 .28000E+01 .37668E+60 157 45 .28000E+01 .13150E-01 158 34 .28000E+01 .13150E-01 160 36 .28750E+01 .13150E-01 161 35 .28750E+01 .13150E-01 162 34 .28750E+01 .55000E+01 163 33 .28750E+01 .55000E+01 164 27 .29500E+01 .57200E-02 165 26 .29500E+01 .57200E-02 166 25 .29500E+01 .57200E-02 167 24 .29500E+01 .53500E+00 168 15 .30000E+01 .35000E+00 169 14 .36000E+01 .35000E+00	127	88	.25000E+01	. 24934E+08
130 85 .25\\000E+01 .77192E+00 131 84 .25000E+01 .10200E+01 132 80 .25750E+01 .29330E-01 133 79 .25750E+01 .12708E+03 134 78 .25750E+01 .24438E+00 135 77 .25750E+01 .38515E+00 136 76 .25750E+01 .55406E+03 137 75 .25750E+01 .75676E+00 138 74 .2750E+01 .75676E+00 139 70 .26750E+01 .10000E+01 139 70 .26500E+01 .27310E-01 140 69 .26500E+01 .27310E-01 141 68 .26500E+01 .36921E+00 142 67 .26500E+01 .36921E+00 144 65 .26500E+01 .36921E+00 145 64 .26500E+01 .72628E+00 146 60 .27250E+01 .23940E-01 147 59 .27250E+01 .23940E-01 148 58 .27250E+01 .22940E-01 149 57 .27250E+01 .35241E+00 150 56 .27250E+01 .35241E+00 151 55 .27250E+01 .50834E+00 152 54 .27250E+01 .50834E+00 153 49 .2300GE+01 .50834E+00 154 48 .28000E+01 .11742E+03 155 47 .2800JE+01 .37668E+60 157 45 .2800JE+01 .37668E+60 157 45 .2800JE+01 .33526E+60 159 37 .28750E+01 .13150E-01 160 36 .28750E+01 .13150E-01 161 35 .28750E+01 .13150E-01 162 34 .28750E+01 .57500E+03 164 27 .29500E+01 .57200E-02 165 26 .29500E+01 .57200E-02 166 25 .29500E+01 .57200E-02 167 24 .29500E+01 .57200E-02 168 15 .30000E+01 .57200E-02 168 15 .30000E+01 .55000E+00 169 14 .36000E+01 .55000E+00	128	87	.2500UE+01	.39290E+00
131 84 .25000E+01 .10200E+01 132 80 .25750E+01 .29330E-G1 133 79 .25750E+01 .12708E+03 134 78 .25750E+01 .38515E+00 135 77 .25750E+01 .55405E+03 136 76 .25750E+01 .55405E+03 137 75 .25750E+01 .75676E+03 138 74 .27750E+01 .10000E+G1 139 70 .26750E+01 .27310E-01 140 69 .25500E+01 .27310E-01 141 68 .26500E+01 .23335E+00 142 67 .26500E+01 .35921E+00 143 66 .26500E+01 .35921E+00 144 65 .26500E+01 .53151E+00 144 65 .26500E+01 .72628E+03 145 64 .26500E+01 .72628E+03 146 66 .27250E+01 .23940E-01 147 59 .27250E+01 .22346E+03 148 58 .27250E+01 .22346E+03 149 57 .27250E+01 .35241E+03 150 56 .27250E+01 .35241E+03 151 55 .27250E+01 .50834E+03 152 54 .27250E+01 .50834E+03 153 49 .2300GE+01 .50834E+03 154 48 .2800E+01 .19220E-01 155 47 .2800JE+01 .37668E+G3 156 46 .2800DE+01 .11742E+03 157 45 .2800JE+01 .37668E+G3 158 44 .23000E+01 .13150E-01 160 36 .28750E+01 .33718E+60 161 35 .28750E+01 .33718E+60 163 33 .28750E+01 .57200E+03 164 27 .29500E+01 .57500E+03 165 26 .29500E+01 .57200E+02 165 26 .29500E+01 .57200E+03 166 25 .29500E+01 .53500E+03 167 24 .29500E+01 .35000E+03 168 15 .3000UE+01 .35000E+03 169 14 .3000UE+01 .35000E+03	129	86	.25000E+01	.56518E+00
132 80 .25750E+01 .29330E-01 133 79 .25750E+01 .12708E+03 134 78 .25750E+01 .24438E+00 135 77 .25750E+01 .38515E+00 136 76 .25750E+01 .55406E+01 137 75 .25750E+01 .75676E+00 138 74 .26750E+01 .10000E+01 139 70 .26750E+01 .12124E+03 140 69 .20500E+01 .23395E+00 141 68 .26500E+01 .36921E+00 142 67 .26500E+01 .35921E+00 144 65 .26500E+01 .72628E+03 145 64 .26500E+01 .23940E-01 146 60 .27250E+01 .23940E-01 147 59 .27250E+01 .23940E-01 148 58 .27250E+01 .22246E+03 149 57 .27250E+01 .35241E+03 149 57 .27250E+01 .35241E+03 150 56 .27250E+01 .5834E+03 151 55 .27250E+01 .5834E+03 152 54 .27250E+01 .5834E+03 153 49 .2300GE+01 .59834E+03 154 48 .28000E+01 .19220E-01 155 47 .2800JE+01 .37668E+63 157 45 .2800JE+01 .37668E+63 158 37 .28750E+01 .33526E+60 169 38 .28750E+01 .594637E+00 161 35 .28750E+01 .594637E+00 162 34 .28750E+01 .575000E+03 164 27 .29500E+01 .575000E+03 166 25 .29500E+01 .57200E-02 165 26 .29500E+01 .57200E-02 166 25 .29500E+01 .35000E+00 168 15 .30000E+01 0.31300E+00 168 15 .30000E+01 0.31300E+00 168 15 .30000E+01 0.313000E+01	130	85	.25600E+01	.77192E+00
132 80 .25750E+01 .29330E-01 133 79 .25750E+01 .12708E+03 134 78 .25750E+01 .24438E+00 135 77 .25750E+01 .38515E+00 136 76 .25750E+01 .55406E+01 137 75 .25750E+01 .75676E+00 138 74 .26750E+01 .10000E+01 139 70 .26750E+01 .12124E+03 140 69 .20500E+01 .23395E+00 141 68 .26500E+01 .36921E+00 142 67 .26500E+01 .35921E+00 144 65 .26500E+01 .72628E+03 145 64 .26500E+01 .23940E-01 146 60 .27250E+01 .23940E-01 147 59 .27250E+01 .23940E-01 148 58 .27250E+01 .22246E+03 149 57 .27250E+01 .35241E+03 149 57 .27250E+01 .35241E+03 150 56 .27250E+01 .5834E+03 151 55 .27250E+01 .5834E+03 152 54 .27250E+01 .5834E+03 153 49 .2300GE+01 .59834E+03 154 48 .28000E+01 .19220E-01 155 47 .2800JE+01 .37668E+63 157 45 .2800JE+01 .37668E+63 158 37 .28750E+01 .33526E+60 169 38 .28750E+01 .594637E+00 161 35 .28750E+01 .594637E+00 162 34 .28750E+01 .575000E+03 164 27 .29500E+01 .575000E+03 166 25 .29500E+01 .57200E-02 165 26 .29500E+01 .57200E-02 166 25 .29500E+01 .35000E+00 168 15 .30000E+01 0.31300E+00 168 15 .30000E+01 0.31300E+00 168 15 .30000E+01 0.313000E+01				
133				
134			.2575UE+01	
135				
136				
137		76	.25750E+01	.55406E+00
139		75	.25750E+01	.75676E+00
139		74	25750E+01	.10000E+61
141 68 .26500E+01 .23395E+00 142 67 .26500E+01 .36921E+00 143 66 .26500E+01 .53151E+00 144 65 .26500E+01 .72628E+00 145 64 .26500E+01 .96000E+00 146 60 .27250E+01 .23940E-01 147 59 .27230E+01 .11418E+03 148 58 .27250E+01 .22246E+03 149 57 .27230E+01 .35241E+00 150 56 .27230E+01 .50834E+00 151 55 .27230E+01 .69546E+G0 152 54 .27230E+01 .92000E+00 153 49 .2300GE+01 .92000E+00 153 49 .2300GE+01 .19220E-01 154 48 .28000E+01 .11742E+03 155 47 .28000E+01 .37668E+G0 157 45 .28000E+01 .37668E+G0 158 44 .23000E+01 .75000E+G1 159 37 .28730E+01 .13150E-01 160 36 .28750E+01 .1316E+00 161 35 .28750E+01 .37718E+00 162 34 .28750E+01 .37718E+00 163 33 .28750E+01 .57200E+03 164 27 .29500E+01 .57200E+03 165 26 .29500E+01 .57200E+02 166 25 .29500E+01 .57200E+02 167 24 .29500E+01 .35000E+00 168 15 .30000E+01 .35000E+03		70	. 2050GE+01	.27310E-01
142 67 .26500E+01 .36921E+00 143 66 .26500E+01 .53151E+00 144 65 .26500E+01 .72628E+00 145 64 .26500E+01 .96000E+00 146 60 .27250E+01 .23940E-01 147 59 .27250E+01 .22246E+00 148 58 .27250E+01 .22246E+00 149 57 .27250E+01 .35241E+00 150 56 .27250E+01 .50834E+00 151 55 .27250E+01 .69546E+G0 152 54 .27250E+01 .92000E+00 153 49 .2300GE+01 .19220E-01 154 48 .28000E+01 .19220E-01 155 47 .28000E+01 .37668E+G0 157 45 .28000E+01 .37668E+G0 157 45 .28000E+01 .75000E+G0 158 37 .28750E+01 .13150E-01 160 36 .28750E+01 .13150E-01 161 35 .28750E+01 .37718E+00 162 34 .28750E+01 .57200E+02 163 33 .28750E+01 .57200E+02 164 27 .29500E+01 .57200E+02 165 26 .29500E+01 .57200E+02 166 25 .29500E+01 .57200E+02 167 24 .29500E+01 .35000E+00 168 15 .30000E+01 .35000E+00 168 15 .30000E+01 .35000E+00	140	69	.25500E+01	.12124E+00
143       66       .26500E+01       .72628E+00         144       65       .26500E+01       .72628E+00         145       64       .26500E+01       .96000E+00         146       60       .27250E+01       .23940E-01         147       59       .27250E+01       .11418E+00         148       58       .27250E+01       .22246E+00         149       57       .27250E+01       .35241E+00         150       56       .27250E+01       .50834E+00         151       55       .27250E+01       .69546E+60         152       54       .27250E+01       .92000E+00         153       49       .2300GE+01       .19220E-01         153       49       .2300GE+01       .19220E-01         154       48       .2800GE+01       .11742E+00         155       47       .2800GE+01       .37668E+G0         157       45       .2800GE+01       .37668E+G0         158       44       .2300GE+01       .7500GE+01         159       37       .2875GE+01       .1315GE-01         160       36       .2875GE+01       .1315GE-01         161       35       .2875GE+01       .5500GE+	141	68	.26500E+01	.23395E+00
144       65       .26500E+01       .72628E+00         145       64       .26500E+01       .96000E+00         146       60       .27250E+01       .23940E-01         147       59       .27250E+01       .11418E+00         148       58       .27250E+01       .22246E+00         149       57       .27250E+01       .35241E+00         150       56       .27250E+01       .50834E+00         151       55       .27250E+01       .69546E+G0         152       54       .27250E+01       .92000E+00         153       49       .2300GE+01       .19220E-01         154       48       .28000E+01       .1742E+03         155       47       .28000E+01       .37668E+G0         157       45       .28000E+01       .37668E+G0         158       44       .23000E+01       .54637E+00         159       37       .28750E+01       .13150E-01         160       36       .28750E+01       .13150E-01         161       35       .28750E+01       .55000E+01         164       27       .29500E+01       .57200E-02         165       26       .29500E+01       .57200E-0	142	67	.26500E+01	.369215+00
145 64 .26500E+01 .96000E+00 146 60 .27250E+01 .23940E-01 147 59 .27250E+01 .11418E+00 148 58 .27250E+01 .22246E+00 149 57 .27250E+01 .35241E+00 150 56 .27250E+01 .50834E+00 151 55 .27250E+01 .69546E+00 152 54 .27250E+01 .92000E+00 153 49 .2300GE+01 .19220E-01 154 48 .28000E+01 .11742E+00 155 47 .28000E+01 .37668E+00 156 46 .28000E+01 .37668E+00 157 45 .28000E+01 .37668E+00 158 37 .28750E+01 .54637E+00 159 37 .28750E+01 .13150E-01 160 36 .28750E+01 .1316E+00 161 35 .28750E+01 .1316E+00 162 34 .28750E+01 .37718E+00 163 33 .28750E+01 .55000E+01 164 27 .29500E+01 .57200E-02 165 26 .29500E+01 .57200E-02 166 25 .29500E+01 .37718E+00 167 24 .29500E+01 .35000E+00 168 15 .30000E+01 .35000E+00 168 15 .30000E+01 .35000E+00 168 15 .30000E+01 .35000E+00	143	66	.26500E+01	.53151E+00
146       60       .27250E+01       .23940E-01         147       59       .27250E+01       .11418E+00         148       58       .27250E+01       .22246E+00         149       57       .27250E+01       .35241E+00         150       56       .27250E+01       .50834E+00         151       55       .27250E+01       .69546E+00         152       54       .27250E+01       .92000E+00         153       49       .23000E+01       .19220E-01         154       48       .28000E+01       .11742E+00         155       47       .28000E+01       .23526E+00         156       46       .28000E+01       .37668E+00         157       45       .28000E+01       .54637E+00         158       44       .23000E+01       .75000E+01         159       37       .28750E+01       .13150E-01         160       36       .28750E+01       .1316E+00         161       35       .28750E+01       .57200E-02         165       26       .29500E+01       .57200E-02         165       26       .29500E+01       .21380E+00         166       25       .29500E+01       .35000E+0	144	65	.26503E+01	.72628E+U0
147       59       .27250E+01       .22246E+00         148       58       .27250E+01       .22246E+00         149       57       .27250E+01       .35241E+00         150       56       .27250E+01       .50834E+00         151       55       .27250E+01       .69546E+00         152       54       .27250E+01       .92000E+00         153       49       .2300GE+01       .19220E-01         154       48       .2800GE+01       .11742E+03         155       47       .2800GE+01       .37668E+G0         156       46       .2800GE+01       .37668E+G0         157       45       .2800GE+01       .54637E+00         158       44       .2300GE+01       .7500GE+01         159       37       .2875GE+01       .1315GE-01         160       36       .2875GE+01       .1315GE-01         161       35       .2875GE+01       .37718E+00         162       34       .2375GE+01       .5720GE-02         163       33       .2875GE+01       .5720GE-02         164       27       .295GGE+01       .2138GE+00         166       25       .295GGE+01       .2138GE+	145	64	.26500E+01	.96000E+00
147       59       .27250E+01       .22246E+00         148       58       .27250E+01       .22246E+00         149       57       .27250E+01       .35241E+00         150       56       .27250E+01       .50834E+00         151       55       .27250E+01       .69546E+00         152       54       .27250E+01       .92000E+00         153       49       .2300GE+01       .19220E-01         154       48       .2800GE+01       .11742E+03         155       47       .2800GE+01       .37668E+G0         156       46       .2800GE+01       .37668E+G0         157       45       .2800GE+01       .54637E+00         158       44       .2300GE+01       .7500GE+01         159       37       .2875GE+01       .1315GE-01         160       36       .2875GE+01       .1315GE-01         161       35       .2875GE+01       .37718E+00         162       34       .2375GE+01       .5720GE-02         163       33       .2875GE+01       .5720GE-02         164       27       .295GGE+01       .2138GE+00         166       25       .295GGE+01       .2138GE+	146	60	.27250E+01	.23940E-01
149       57       .27250E+01       .35241E+00         150       56       .27250E+01       .50834E+00         151       55       .27250E+01       .69546E+00         152       54       .27250E+01       .92000E+00         153       49       .2300GE+01       .19220E-01         154       48       .28000E+01       .11742E+00         155       47       .28000E+01       .37668E+G0         156       46       .28000E+01       .37668E+G0         157       45       .28000E+01       .54637E+00         158       44       .23000E+01       .75000E+00         159       37       .28750E+01       .13150E-01         160       36       .28750E+01       .13150E-01         161       35       .28750E+01       .23317E+00         162       34       .23750E+01       .55000E+01         163       33       .28750E+01       .57200E-02         165       26       .29500E+01       .21380E+00         166       25       .29500E+01       .35000E+00         167       24       .29500E+01       .35000E+00         168       15       .30000E+01       .10000E+	147	59	.27250E+01	
150	148	58	.27250E+01	. 22246E+01
151 55 .27250E+01 .69546E+G0 152 54 .27250E+01 .92000E+00 153 49 .2300GE+01 .19220E-01 154 48 .28000E+01 .11742E+03 155 47 .28003E+01 .23526E+G0 156 46 .28000E+01 .37668E+G0 157 45 .28003E+01 .54637E+00 158 44 .23000E+01 .75000E+03 159 37 .28750E+01 .13150E-01 160 36 .28750E+01 .1316E+00 161 35 .28750E+01 .23317E+00 162 34 .23750E+01 .37718E+60 163 33 .28750E+01 .55000E+03 164 27 .29500E+01 .57200E-02 165 26 .29500E+01 .57200E-02 166 25 .29500E+01 .21380E+00 167 24 .29500E+01 .35000E+00 168 15 .30000E+01 0.	149	57	.27250E+01	.35241E+00
152       54       .27250E+01       .92000E+00         153       49       .2300GE+01       .19220E-01         154       48       .28000E+01       .11742E+03         155       47       .28000E+01       .23526E+G0         156       46       .28000E+01       .37668E+G0         157       45       .28000E+01       .54637E+00         158       44       .23000E+01       .75000E+03         159       37       .28750E+01       .13150E-01         160       36       .28750E+01       .13150E-01         161       35       .28750E+01       .23317E+00         162       34       .28750E+01       .37718E+60         163       33       .28750E+01       .55000E+01         164       27       .29500E+01       .57200E-02         165       26       .29500E+01       .21380E+00         166       25       .29500E+01       .35000E+00         167       24       .29500E+01       .35000E+00         168       15       .30000E+01       .10000E+03	150	56	.27250E+01	.50834E+00
152       54       .27250E+01       .92000E+00         153       49       .2300GE+01       .19220E-01         154       48       .28000E+01       .11742E+03         155       47       .28000E+01       .23526E+G0         156       46       .28000E+01       .37668E+G0         157       45       .28000E+01       .54637E+00         158       44       .23000E+01       .75000E+03         159       37       .28750E+01       .13150E-01         160       36       .28750E+01       .13150E-01         161       35       .28750E+01       .23317E+00         162       34       .28750E+01       .37718E+60         163       33       .28750E+01       .55000E+01         164       27       .29500E+01       .57200E-02         165       26       .29500E+01       .21380E+00         166       25       .29500E+01       .35000E+00         167       24       .29500E+01       .35000E+00         168       15       .30000E+01       .10000E+03	151	55	.27250E+01	.69546E+00
154	152	54	.27250E+01	.92000E+00
155	153	49	.2300GE+01	.19220E-01
156	154	48	.28000E+01	.11742E+03
157	155	47	.2800JE+01	.23526E+G0
158	156	46	.28000E+01	.37668E+G0
159 37 .28750E+01 .13150E-01 160 36 .28750E+01 .11316E+00 161 35 .28750E+01 .23317E+00 162 34 .28750E+01 .37718E+00 163 33 .28750E+01 .55000E+00 164 27 .29500E+01 .57200E-02 165 26 .29500E+01 .10030E+00 166 25 .29500E+01 .21380E+00 167 24 .29500E+01 .35000E+00 168 15 .30000E+01 0.	157	45	.2800JE+01	.54637E+00
160 36 .2875 0E+01 .11316E+00 161 35 .2875 0E+01 .23317E+00 162 34 .2875 0E+01 .37718E+00 163 33 .2875 0E+01 .550 00E+00 164 27 .2950 0E+01 .572 00E-02 165 26 .2950 0E+01 .100 30 E+00 166 25 .2950 0E+01 .2138 0E+00 167 24 .2950 0E+01 .350 00E+00 168 15 .30 00 0E+01 0.	158	44	.23000E+01	
161 35 .2875 UE+01 .23317E+00 162 34 .2675 OE+01 .37718E+C0 163 33 .2875 UE+01 .550 OOE+0J 164 27 .295 OOE+01 .572 OOE-02 165 26 .295 OOE+01 .100 30 E+00 166 25 .295 OOE+01 .2138 OE+00 167 24 .295 OOE+01 .350 OOE+00 168 15 .30 OO UE+01 0.	159	37	.28750E+01	.13150E-01
162       34       .28750E+01       .37718E+60         163       33       .28750E+01       .55000E+00         164       27       .29500E+01       .57200E-02         165       26       .29500E+01       .10030E+00         166       25       .29500E+01       .21380E+00         167       24       .29500E+01       .35000E+00         168       15       .30000E+01       0         169       14       .3C000E+01       .10000E+03	163	36	.2875 DE+01	.11316E+00
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                                                                                                                                                                                                                                                                                      2.125E+00
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                                                                                                                                                                                                               3.497E+00
                                                                                                                                                                                                                                                    5.000E+00
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9						144	111	61	31	S	140	109	87	65	36	
52			168	•		157	133	73	30	m	141	110	88	99	37	
5			164	E-02	E-02	156	126	72	53	N.	142	115	68	67	44	
48			159	1.794E-C	-6.022	155	125	71	<b>58</b>	o	143	116	96	68	45	
<b>4</b>			153	E-02	E-01-	154	124	83	36	50	149	117	96	<b>69</b>	46	
42			146	3.589E-												
36			139	F-02	-05-31	165	122	81	42	10	151	119	96	74	48	13
36			132	S	-9.004	164	138	93	4 1	<b>3</b> 0	152	120	4	75	49	14
35		85	S	N	à	Ŋ	1	Ñ	Ó	7	0	-	œ	Q	4	S
31		84	118	7.193E-0	-7.193	162	136	16	38	18	159	127	66	1:	52	24
56		83	111	-02	-02	161	135	103	53	23	160	128	100	78	56	25
				9.004E	IJ											
76	16	Z	86	2E-01	-20-3	170	148	101	51	19	-	130	105	80	58	27
1 .	71	4	56	1.082E	-3,589	167	147	114	20	17	4	131	106	84	56	33
9	99	٣	89	6.022E-02	1E-02-	168	146	113	63	16	1 1	132	107	85	9	34
-	61	<b>⊘</b>	90	6.022	1.794	167	145	112	62	32	22	139	108	86 85 84 8	64	35

## 5.1.2 STRANL-II Program

With the present mesh, three cases of freestream Mach numbers are to be computed. These are

$$M_{\infty} = 0.806$$
 (Subcritical)  
 $M_{\infty} = 0.861$  (Barely Critical)  
 $M_{\infty} = 0.909$  (Supercritical)

## Input

Listed below are typical input cards to the STRANL-II program to compute flow field for the above cases.

The above cards indicate there is no non-zero initial guess furnished in order to compute the case  $M_{\infty} = 0.806$ , while cases with higher Mach number will use results computed for lower Mach number as initial guess. In all cases, the nonlinear boundary condition on the actual airfoil surface is to be used, as suggested by IOPT (3) = 0 in the options card.

## Output

The output from this program includes printouts and punch cards for the convergent solution(s).

The printouts are in the following order:

- Title of the problem under study
- Convergent limit
- Control keys specified in the options card
- Total number of elements, number of nodal points, and the full bandwidth of the resulting matrix equations
- Element numbers and element node points
- Nodal numbers and their corresponding x- and y-coordinates
- Boundary nodes for each type of boundary
- Slope for nodes on the airfoil surface
- For each iteration, the computed results at all nodal points are printed, together with a printer plot displaying the pressure coefficient on the airfoil surface.

The above items except problem parameters and computed results have also been printed in the STRANL-I program, but are repeated here for completeness. For brevity, only results for a typical iteration are listed on the next five pages for reference.

# 5.2 Flow Over a NACA 64 A006 Airfoil

This problem was analyzed using the mesh shown in Sketch 2, which consists of 120 quadrilaterals with 150 nodes. For this particular mesh, it is apparent that nodal numbering along the shorter (vertical) direction yields the smallest bandwidth and, therefore, no nodal renumbering is required. Since the present mesh has a rather regular pattern, less input cards are required. The procedures described for the circular arc airfoil problem also applied here. For brevity, only the input cards to both programs and some typical printouts from STRANL-II are listed here for reference. Again, the nonlinear boundary condition on the actual airfoil surface is to be used in computations for all the cases.

MACH NUMBER = . 909 PELAX. FACTOR = .5008

0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0	1110	#CO!	VCCM	COF	LMAC	04/4	Ţ	DELM
6.2939E-01 9.106E-01 5.845E-01 3.131E-02 0.	•				•	5.44545-01	٠,	Ľ
0. 6.0166-04	1		•	10 10000		ALCHE-01	-4-1341F-NZ	3-2793E-06
7.9639E-04 8.2625E-01 9.9109E-01 5.8550E-01 1.4401E-01 0.2.6900E-04 8.2625E-01 9.1010E-01 5.8550E-01 1.4401E-01 0.2.6900E-04 8.2625E-01 9.1010E-01 5.8550E-01 1.334E-01 1.9000E-03 3.1010E-03 3.1010E-	1.0016E+00		•	8 - 29 39 E = U I	9-0388E-01	5.88775-91	9. E736E-03	2.5974E-05
6.8178E-01 6.315E-01 5.345E-01 1.4461E-01 6.3465E-01 1.4461E-01 6.3165E-01 1.4461E-01 1.6901E-04 8.2626E-01 9.0451E-01 5.4661E-01 1.99016E-01 3.5162E-01 1.59016E-01 1.59	70 32705 0		•	7 96496-01	8. 93.09F-01	5.956 9E-01	3.3119E-02	-1.04796-15
8.2626E-01 9.0910E-01 5.8550E-01 1.0908E-03 8.2825E-01 9.0910E-01 5.8550E-01 1.0908E-03 8.2825E-01 9.0410E-01 5.8550E-01 1.0708E-03 8.2825E-01 9.0410E-01 5.8550E-01 1.0708E-03 8.2825E-01 9.0410E-01 5.8550E-01 1.0708E-03 8.2825E-01 9.0908E-01 5.8550E-01 1.0708E-03 8.2825E-01 9.0908E-01 5.8550E-01 1.0705E-01	9-0493E-91		• •	6.8178E-01	8.3315E-01	6.3445E-01	.4481E-0	-3.5696F-05
8.2025F-01         9.100FE-01         5.44R2-01         -1.990RE-03           7.3172FE-01         9.9019F-01         5.4886E-01         3.002FE-02           7.3172FE-01         9.903FE-01         5.9786E-01         3.003FE-02           8.202FE-01         9.903FE-01         5.8786E-01         1.373FE-01           8.202FE-01         9.903FE-01         5.8786E-01         1.373FE-01           8.202FE-01         9.903FFE-01         5.8786E-01         1.373FE-01           8.202FE-01         9.903FFE-01         5.8786E-01         1.373FE-01           8.202FE-01         9.903FFE-01         5.8786E-01         1.373FE-01           8.202FE-01         9.903FE-01         5.8786E-01         5.305FE-01           8.202FE-01         9.903FE-01         5.877FE-01         6.316FE-02           8.202FE-01         9.903FE-01         5.877FE-01         6.317FE-02           8.202FE-01         9.903FE-01         5.857FE-01         6.477FE-02           8.202FE-01         9.903FE-01         5.857FE-01         7.83FE-02           8.202FE-01         9.903FE-01         5.87FE-01         7.93FE-02           8.202FE-01         9.903FE-01         5.87FE-01         7.93FE-02           8.202FE-01         9.903FE-01         5.	1.000F+00			8.2628E-01	9.0930E-01	5.8550E-01		•
\$\begin{array}{c} 5.9028E-05 & 0.1726E-01 & 0.9449E-01 & 5.978E-01 & 0.1916E-03 & 0.1766E-04 & 0.9951E-01 & 5.978E-01 & 1.3736E-01 & 0.9951E-01 & 5.978E-01 & 1.086E-01 & 0.9951E-01 & 5.978E-01 & 0.9951E-01 & 0.	1.0010F+00		-2.6900E-04	8.2825F-01	9.100 FE-01	5.84R2E-01	-1 - 690 BE-03	2 -9 173 E-36
7. 9152E-01 8.9051E-01 5.975E-01 3.5012E-72 8.262BE-01 9.0998E-01 5.8457E-01 -1.3734E-01 8.262BE-01 9.0998E-01 5.8457E-01 -1.3734E-01 8.262BE-01 9.0998E-01 5.8457E-01 -1.3734E-02 7.9345E-01 9.0998E-01 5.8457E-01 3.3057E-02 7.9345E-01 9.0998E-01 5.8557E-01 3.3057E-02 7.9345E-01 9.0998E-01 5.8557E-01 0.0865E-01 8.262BE-01 9.0994E-01 5.8557E-01 0.3709E-04 8.262BE-01 9.0994E-01 5.8557E-01 0.3709E-04 8.262BE-01 9.0996E-01 5.8557E-01 7.8722E-02 7.4776ZE-01 9.0906E-01 5.8557E-01 7.8722E-02 7.4776ZE-01 9.0906E-01 5.8557E-01 7.8722E-02 8.262BE-01 9.0906E-01 5.8557E-01 3.6456E-03 8.262BE-01 9.0906E-01 5.8557E-01 7.8726E-02 8.262BE-01 9.0906E-01 5.8557E-01 7.036E-02 8.262BE-01 9.0906E-01 5.8557E-01 7.036E-03 8.262B	9.9545E-01		5. 9023E-05	8.1726E-01	9.0419E-01	5.8858E-01	9.0918E-03	1.2897E-36
6.818E-01	9.8247E-01		-3.1468E-04	7.9152E-01	8.9051E-01	5.9735E-01	3.5092E-12	-1.1/24E-35
8.2612E-01 9.0907E-01 5.8550E-01 -1.8552E-03 7.262E-03 8.2024E-01 9.0997E-01 5.8550E-01 1.0005E-03 7.5526E-03 7.5526E-03 7.5526E-01 1.0005E-03 7.5526E-03	9.3087E-61		9. 7688E-03	6.8918E-01	8.37 03E-01	6.31935-01	. 3734E-E	-3.8960£-05
8,2012E-01 9,099RE-01 5,848RE-01 -1,852E-03 7,934SE-01 8,0154E-01 5,966SE-01 3,3157E-02 7,934SE-01 9,057RE-01 5,966SE-01 1,006SE-01 3,3157E-02 8,271E-01 9,057RE-01 5,855DE-01 1,006SE-03 7,934SE-01 9,094KE-01 5,857DE-01 -0,370SE-02 7,877E-01 9,094KE-01 5,877DE-01 -0,370SE-02 7,877E-01 9,094KE-01 5,877DE-01 -0,370SE-02 7,877E-01 9,094KE-01 5,875DE-01 7,875SE-02 7,877E-01 9,090RE-01 5,855DE-01 7,875SE-02 7,875E-01 9,090RE-01 5,855DE-01 7,03SE-02 7,875E-01 9,090RE-01 5,855DE-01 3,845SE-02 7,845GE-01 9,090RE-01 5,855DE-01 3,845SE-02 7,845GE-01 9,090RE-01 5,855DE-01 1,470SE-02 8,267E-01 9,090RE-01 5,855DE-01 1,470SE-03 8,267E-01 9,090RE-01 5,855DE-01 1,470SE-02 8,267E-01 9,090RE-01 5,855DE-01 1,470SE-03 8,267E-01 9,090RE-01 5,855DE-01 1,470SE-02 8,267E-01 1,470SE-01 1,470SE-01 1,470SE-02 8,267E-01 1,470SE-01	1.0900E+00		0.	8.2628E-01	9.8 900E-01	5.855 CE-01	. 0-	
8,2026-01 9,0578-01 5,0556-91 5,0505-02 7,93456-01 9,0578-01 5,0596-01 1,0066-01 7,18030-01 9,0946-01 5,0596-01 1,0066-01 8,2716-01 9,0946-01 5,0576-01 3,03776-01 7,4762-01 9,0946-01 5,0576-01 7,03776-01 8,2716-01 9,0946-01 5,0576-01 7,03726-02 8,2716-01 9,0946-01 5,0576-01 7,03726-02 8,2716-01 9,0946-01 5,0576-01 7,0376-02 8,2716-01 9,0946-01 5,0576-01 7,0376-02 8,2716-01 9,0946-01 5,0576-01 3,0456-02 7,9726-01 9,0946-01 5,0576-01 7,0376-02 8,2676-01 9,0946-01 5,0576-01 7,0376-02 8,2676-01 9,0946-01 5,0576-01 7,0376-02 8,2676-01 9,0946-01 5,0576-01 1,0406-02 8,2676-01 9,0946-01 5,0576-01 1,0406-02 8,2676-01 9,0946-01 5,0576-01 1,0476-02 8,2676-01 9,0946-01 5,0576-01 1,0476-02 8,2676-01 9,0946-01 5,0576-01 1,0476-02 8,2676-01 9,0946-01 5,0576-01 1,0476-02 8,2676-01 9,0946-01 5,0576-01 1,0476-02 8,2676-01 9,0946-01 5,0576-01 1,0476-02 8,2676-01 9,0946-01 5,0576-01 1,0476-02 8,2676-01 9,0946-01 5,0576-01 1,0476-02 8,2676-01 9,0946-01 5,0576-01 1,0476-02 8,2676-01 9,0976-01 5,0576-01 1,0476-02 8,2676-01 9,0976-01 5,0576-01 1,0476-02 8,2676-01 9,0976-01 5,0576-01 1,0476-02 8,2676-01 9,0976-01 5,0576-01 1,0476-02 8,2676-01 9,0976-01 5,0576-01 1,0476-02 8,2676-01 9,0976-01 5,0576-01 1,0476-02 8,2676-01 9,0976-01 5,0576-01 1,0476-02 8,2676-01 9,0976-01 5,0576-01 1,0476-02 8,2676-01 9,0976-01 5,0676-01 1,0476-02 8,2676-01 9,0976-01 5,0676-01 1,0476-02 8,2676-01 9,0976-01 5,0676-01 1,0476-02 8,2676-01 9,0976-01 5,0676-01 1,0476-02 8,2676-01 9,0976-01 5,0676-01 1,0476-02 8,2676-01 9,0976-01 5,0676-01 1,0476-02 8,2676-01 9,0976-01 5,0676-01 1,0476-02 8,2676-01 9,0976-01 5,0676-01 1,0476-02 8,2676-01 9,0976-01 5,0676-01 1,0476-02 8,2676-01 9,0976-01 5,0676-01 1,0476-02 8,2676-01 9,0976-01 5,0676-01 1,0476-02 8,2676-01 9,0976-01 5,0676-01 1,0476-02 8,2676-01 9,0976-01 5,0676-01 1,0476-02 8,2676-01 0,0976-01 5,0676-01 1,0476-02 8,2676-01 0,0976-01 5,0676-01 1,0476-02 8,2676-01 0,0976-01 5,0676-01 1,0476-02 8,2676-01 0,0976-01 5,0676-01 1,0476-02 8,2676-01 0,0976-01 5,0676-01 1,0476-02 8,2676-01 0,0976-01 5,0676-01 1,0476-02	1. 3009E+00		-2.5953E-84	8.2812E-01	9.0998E-01	5.8487E-01	-1.8552E-03	2.7.15/E-06
7.9345E-01 8.9154F-01 5.9669E-01 3.3077F-97 7.9345E-01 9.0944E-01 5.8591E-01 1.0006E-01 8.2711E-01 9.0944E-01 5.8591E-01 -0.3009E-04 8.1962E-01 9.0944E-01 5.8591E-01 -0.5150E-02 8.1962E-01 9.0946E-01 5.8591E-01 7.8326E-02 8.2712E-01 9.0945E-01 5.8591E-01 7.8326E-02 8.2712E-01 9.0945E-01 5.8591E-01 7.8326E-02 7.84764E-01 9.0945E-01 5.8591E-01 3.6456E-03 7.84764E-01 9.0945E-01 5.8591E-01 3.6456E-03 7.8416E-01 9.0945E-01 5.8591E-01 3.6456E-03 8.2267E-01 9.0907E-01 5.8591E-01 3.6456E-03 8.2626E-01 9.0907E-01 5.8591E-01 3.6456E-03 8.2626E-01 9.0907E-01 5.8591E-01 2.4646E-02 8.2626E-01 9.0907E-01 5.8591E-01 2.4646E-02 8.2626E-01 9.0907E-01 5.8591E-01 7.6502E-03 8.2626E-01 9.0907E-01 5.8591E-01 7.6491E-03 8.2626E-01 9.0907E-01 5.8591E-01 7.6502E-03 8.2626E-01 9.0907E-01 5.8591E-01 1.47476E-03 8.2626E-01 9.0907E-01 5.8591E-01 1.47476E-03 8.2636E-01 9.0907E-01 5.8591E-01 1.4574E-03 8.2636E-01 9.0907E-01 5.8591E-01 1.3531E-01 1.353	9.9695E-01		7.4553E-04	8.2024E-01	9.057 PE-01	5.8756E-91	6.085E-83	1.0 5955-40
7.1830E-01 8.5226E-01 5.6220E-01 1.0000E-01 7.0000E-01 9.0944E-01 5.6250E-01 0.0944E-01 5.6250E-01 0.0944E-01 5.6550E-01 0.0945E-01 0.0944E-01 5.6550E-01 0.0945E-01 0.0946E-01	9.8345E-01		1.7844E-83	7.9345E-01	8.9154F-01	5. 9669E-31	3.3357E-02	-4.2 256E-36
# 2626E 01 9.090E 01 5.8521E 01 1.0.3709E 04 8.271E 01 9.090E 01 5.8571E 01 3.871E 02 0.855E 03 0.855E 01 3.871E 01 3.871E 02 0.855E 03 0.855E 01 3.871E 01 3.871E 02 0.8770E 01 3.871E 02 0.8770E 01 3.871E 02 0.8770E 01 3.871E 02 0.8770E 01 0.871E 02 0.8770E 01 0.871E 02 0.8770E 01 0.871E 02 0.871E 02 0.871E 02 0.871E 01 0.87	9.4555E-11		1.8065E-02	7.1830E-01	8-5226E-31	5.2205E-01	1.00055-01	C9 - 120000 00 - 0
\$\begin{array}{c} 8.271E=01 & 9.094E=01 & 5.077E=01 & 5.91E=02 \\ 7.4762E=01 & 0.0946E=01 & 5.967E=01 & 5.91E=02 \\ 8.2712E=01 & 9.0945E=01 & 5.967E=01 & 5.991E=02 \\ 8.2712E=01 & 9.0945E=01 & 5.967E=01 & 5.991E=02 \\ 8.2712E=01 & 9.0945E=01 & 5.957E=01 & 5.991E=02 \\ 8.2712E=01 & 9.0945E=01 & 5.957E=01 & 3.6956E=02 \\ 7.9416E=01 & 9.0945E=01 & 5.957E=01 & 3.6956E=02 \\ 8.2626E=01 & 9.090E=01 & 5.9957E=01 & 4.1821E=02 \\ 8.2626E=01 & 9.090E=01 & 5.9957E=01 & 7.036E=02 \\ 8.2626E=01 & 9.090E=01 & 5.957E=01 & 5.9556E=02 \\ 8.2626E=01 & 9.090E=01 & 5.957E=01 & 2.6646E=02 \\ 8.2626E=01 & 9.090E=01 & 5.957E=01 & 7.6966E=02 \\ 8.2626E=01 & 9.090E=01 & 5.957E=01 & 7.6966E=02 \\ 8.2626E=01 & 9.090E=01 & 5.857E=01 & 7.696E=02 \\ 8.2626E=01 & 9.090E=01 & 5.857E=01 & 7.697E=02 \\ 8.2626E=01 & 9.090E=01 & 5.857E=01 & 7.697E=02 \\ 8.2626E=01 & 9.097E=01 & 5.857E=01 & 7.697E=02 \\ 8.2626E=01 & 9.090E=01 & 5.857E=01 & 7.857E=02 \\ 8.2626E=01 & 9.090E=01 & 5.857E=01 & 7.857E=02 \\ 8.2626E=01 & 9.090E=01 & 5.857E=01 & 7.857E=02 \\ 8.2626E=01 & 9.090E=01 & 5.857E=01 & 7.857E=01 \\ 8.2626E=01 &	1.0000E+00		.0	A. 2628E-01	3.090CE-01	5.8550E-01	-0.	0.0 0.000 FT - 06
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A.1456E-01         9.0200E-01         5.0946E-01         1.1715E-02           8.2645E-01         9.0821E-01         5.850E-01         1.4905E-03           8.2653E-01         9.0859E-01         5.8550E-01         7.6502E-04           8.2656E-01         9.0859E-01         5.8596E-01         7.6502E-04           8.2620E-01         9.0901E-01         5.8596E-01         4.6575E-03           8.2620E-01         9.0901E-01         5.8596E-01         4.4697E-04           8.2620E-01         9.1867E-01         5.8596E-01         1.4474E-02           8.5620E-01         9.1806E-01         5.8591E-01         7.5882E-02           8.5302E-01         9.1806E-01         5.8591E-01         7.5882E-02           8.5302E-01         9.1806E-01         5.8591E-01         -7.5882E-03           8.5302E-01         9.1806E-01         5.8591E-01         -1.4538E-02           8.53771E-01         9.2766E-01         5.8591E-01         -1.1538E-02           8.576E-01         9.2766E-01         5.8159E-01         -1.1538E-02			2-1401E-03	8.2267E-£1	9-87076-01	5.8673E-01	. 6485E-0	-7 -3 275 E-U/
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9. 5.7650E-04 8.3771E-01 9.4511E-01 5.8159E-01 -1.153E-12 1.6916E-03 8.6107E-01 9.2746E-01 5.81540E-01 -3.5140E-02	1.015JE+00		7.9555E-0 4	8.5502E-01	9.2498E-01	5.75*16-91	********	-5.7 354E-E5
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TO THE TOTAL			5.7650E-04	8.3771E-81	9-1511E-01	5-61546-51	26-36-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1	-6. 56 TSE- PS
	1.0175E+00		1.6916E-03	8. 5187E-01	10-30412 %	TOLLDEGUE.	30-13476-0-	1000000

9. 9079F-05	-7 63636-06	-3-0 (0CE-02	6.2856E-06	5.5844E-05	6.6903E-05	٥.	בר. הישמבר הי	5.7358E-06	4.5936E-05	1.7 08 6E-04	••	••	-2.7257E-06	1. 3014E-07	1.58ANF-06	0.	-4.2541E-06	-1.4 984E-06	3.2954E-05	1.2677E-04	••	-6.5350E-06	-3.7966E-16	2.9262E-05	1.7839E-04	-6 72645-06	- 6. 5 20 7E - 05	2.8 T30F-05	0.75685-(5	.0	-6.2440E-05	-1.0079E-05	2.8015E-05	-6 1602E-05	-5.8185E-05	-6.7 060E-05	-7.5702E-95	-7 -8 001E-05	-7.5712E-05	-7.1520E-05	-8.9 345E-05	-9.2748E-05	754E-	-8.4593E-05	: :	- 36 05	-1.0541E-04	- 4. 9056E-05
-9.	-1 744 05-02	-0-	3.5447F-03	7.5U72E-03	-3.5626E-02	-9.	4.808cF-04	7.2229E-04	1.2359E-02	-1.7063E-02		i	3.8529E-04	2 7446-03	2.7840F-02	-9.	3.7510E-04	4.0923E-03	3.8561F-02	5.2351E-02	-9.	-5.3137E-04	5 -0458E-03	2.9467E-02	8 -3542E-UZ	-1 11065-07	0-67856-07	2-4256F-02	1.2558E-01	-0.	-2.378 6E-03	1.1614E-02	1.8489E-02	1.3401E-01	1.7246E-01	1.0904E-01	2.1004E-01	1.23995-01	9.1281E-32	6 - 1327E-02	1.7461E-02	5.1367F-02	3.9162E-02	1.47805-02	-8-4286F-02	-4.5199E-02	-1.8986E-02	-1.2062F-02
5.8550E-01 5.8374E-01	5.74055-04	5.8559E-01	5.8670E-01	5.8804E-01	5.7343E-01	5. 8550E-01	5.8566E-01	5.8794E-01	5.8968E-01	5.7972E-01	5.8550E-01	5.8550E-01	5.8563E-01	5.0475F-01	5.9492F-01	5.8550E-01	5.8562E-01	5.8688E-01	5. 9855E-01	6.0322E-01	5.8550E-11	5.8532E-01	5.8755E-01	5.954 RE-01	5-1570E-01	5.8550E-91	5.8876F-01	5.9371F-01	6.27965-11	5.855GE-01	5.8469E-01	5.8943E-01	5-9176E-01	10-30100G	6.4368E-01	6.2236E-01	5.5604E-01	6.2735E-01	6.1635E-01	6.0624E-01	5. 9139E-01	6.0285E-01	5.98745-01	5. 9050F-01	5.5703E-01	5.7022F-01	5.790 8E-01	5-8142E-31
9.1175E-01	9.2696F-01	9.0900E-01	9.0712E-01	9.0503E01	9.27 92E-01	9.09 DDF-01	9.0874E-01	9.0518E-01	9.0246E-01	9.1505E-01	9.0900E-01	9.0900E-01	9.0880E-01	8. 94.57E-01	8.9429E-01	9.090CE-01	9.0880E-01	9.0664E-01	8.8864E-01	8.8140E-01	9.0900E-C1	9.09 28E-01	9.05 80E-01	8.9343E-01	0.5515E-01	9.0900E-01	9. 039nF-01	8-961RE-01	8.4314E-91	9.09 00E-01	9.10 26E-01	9.0256E-11	8. 3834F-01	7.79575-01	8-1896E-01	8.5178E-01	7.9997E-01	8.4408E-01	8.6106E-01	8.7570E-01	8.99 EUE-01	8.8197E-01	8 OLE 25-01	9.011AF-01	9.5385E-01	9.3299E-01	9.1906E-91	9-15396-01
8.3141E-01	8.59736-01	8.2628E-01	8.2276E-01	8.1875E-01	8.6141E-01	8.2625E-01	8. 258JE-01	8.1911E-01	8.1395E-01	8.4283E-01	8.2628E-01	0. Ch28E-U1	8.2590E-01	7.9913F-01	7.9820E-01	8.2628E-01	8.2591 E-31	8.2223E-01	7.8797E-01	7.7373E-01	8.2628E-C1	8-2681E-01	8. 2028E-01	7.9702E-01	8 25285-01	A-2719F-01	8-1672F-01	8-9220E-01	7.0102E-01	8 -26 28 E-01	3.2864E-01	8-14/6E-01	6. 9182F-01	5-7360F-01	6.5127E-01	7.1579E-01	6.0673E-01	6.9853E-01	7.3267E-01	7. 6353E-01	8.0110E-01	7.6961E-01	7.97005-01	8-1032E-01	9.0405E-01	8. 6669E-01	8.4187E-01	8. 3613E-01
-5.0687E-03	-5.5606E-03		-2.6220E-03	-8.4278E-03	-1.2062E-02	.,	-1.5737E-04	-1.725/E-U3	-8.3914E-03	-1.8917E-UZ	•	7 77077 27	-9.0767E-05	-6.0436F-03	-2.1100E-02	0.	1.98835-04	-5.966E-04	-3.0546E-03	-2.3000E-02		4.0547E-04	-9.58/UE-U4	-1.38/1E-03	30-36-67-0	3. 0981F-04	-6.0301E-04	1.1098E-03	-7.7255E-03	ė		• •	:	5.2547F-02	5.1871E-02	4.3064E-02	9.6221E-02	6.4258E-02	5.2329E-02	4.2244E-02	5.5897E-02	7.3789E-02	4. 5467F-02	3.6061E-02	7.4751E-02	6.61485-02	5.7071E-02	4.6142E-02
1.0026E+00	1.0169E+00	1.0000E+00	9.9822E-01	9.9621E-01	1.0177E+00	1.0000E+00	9.09746-01	10-36266	9.9378E-01	1.0083E+00	1.0000E+00	00436000	9.991E-01	9.8631F-01	9.8584E-01	1.0000€+00	9. 9981E-01	9.9796E-01	9.8068E-01	9.7350E-01	1.000 UE +00	1.000 SE+00	9.96965-01	9.5794F-01	1.00005	1.0006F+00	9.9518E-01	9.8786E-01	9.3684E-01	1.0000E+00	1.0012E+00	9.94196-01	9.3220F-01	8.7258E-01	9.1175E-01	9. 442 BE-01	8.8929E-01	9.3558E-01	5.5280E-01	9.6836E-01	2. 67.5 UE - U.I.	9.715/E-01	9.8524F-01	9.9195E-01	1.0392E+0C	1.0204E+09	1.00796+00	1.0050E+00
1.0310E-03	8.2268E-04		3.6270E-04	2.6511E-03	3.9623E-03		5.4331F-05	7. 1991E-04	4.0035E-03	6.4627E-US	•		5.3027F-04	4.9490E-03	1.2316E-02	0.	8.1673E-07	6.5559E-04	5.0795E-03	1.5946E-02		-1.0952E-04	**************************************	1.9426F-02	0.	-2.4236E-04	8.6454E-04	4.1335E-03	1.9262E-02	•	-2.9877E-04	4.0472E-03	1.9666E-02	-4.3498E-02	-3.8 062E-02	-3.2317E-02	-4.9289E-02	-4.1824E-02	-3.5193E-UZ	-2.8842E-02	70-3526-07	-3.66356-02	-2.9352E-02	-2.2360E-02	-5.119 CE- C2	-4.4272E-02	-3.6988E-02	-2.9713E-02
6,	20	51	25	53	24	22	52		20	60	•	10	63	19	65	99	29	99	60	2:		21	2 :	212	1,4	12	78	62	90	81	82	200	85	98	87	88		3:		25	200	96	96	. 16	96	66		01

• • •	-2.2652F-112	1.3035E+00	3.7322E-02	8.3323E-01	9.1345E-01	5.8265E-01	-8-4058E-03	-6.95/1E-05
	-1-5989F-02	1.0027E+00	2.8856E-02	8.3171E-01	9.1234E-01	4.8336E-UI	-6-3141E-03	10 312000
	-1. CEG4E-02	1 . PR 00F+0C	5.8 19 9E-02	9. 84.83E-01	9.971 PE-01	5.3002E-01	-1 -0 44 0E -01	10-134-0-
***	14. 1423F-02	1.06105+00	5.5536E-02	9.4719E-01	9.7618E-C1	5.4305F-01	-1.256/E-31	1.23435-04
102	20-1451	100411100	5.0497F-02	9-1379E-01	9.5759E-01	5.5458E-01	-9.1147E-02	-1.1 545E - 04
201	-3.3674E-02	1 0001 600	4-4442F-02	8.8394E-01	9.4106E-01	5.6511E-01	-6."277E-02	-1.1930E-04
101	20-34646-2-	1 02045400	T. GREWF-02	A.6666E-01	9.3139E-01	5.7123E-91	-4.2155E-02	-1.1099E-04
1.38	-2.3123E-02	10041414	2.9659E-02	8.5426E-01	9.2446E-01	5.7564E-01	-2.91325-02	10.69.0-
109	-1.6935E-UZ	00111100	2 2422E-02	8.4.295F-01	9.1819E-01	5.79636-31	-1.7336E-02	-7.2532E-05
110	-1.1169E-02	1.1125500	3.99535-02	1.0508E+00	1.0333E+00	5.0793E-01	-2.3022E-01	-1.7175E- 04
11:	26-31616-6-	100225400	4.0630F-02	1.0091E+00	1.0099E+00	5.2221E-01	-1.8755E-01	-1.6846E-04
112	-3.5392E-32	1.09225400	3.9761F-02	9.7076E-01	9.8843E-01	5.3543E-01	-1.4820E-01	-1.5876E-04
113	-3.094/E-02	1.054.65400	1.6473F-02	9.3455E-01	9.6833E-01	5.4795E-01	-1.1104E-01	-1.3849E-04
114	-2.5675E-02	1 03405404	3.14835-02	9-0164E-01	9.5015E-01	5.59366-01	-7.7242E-02	-1.25 ENE - 74
113	20-30-01	1 02575400	2.5234E-02	A.7638E-01	9.3626E-01	5.6814E-31	-5.1276E-02	-1.026 DE- 04
116	-1.4022E-02	1. C168F+00	1.8938E-02	8.5559E-01	9.2490 E-01	5.7536E-01	-2.9954E-02	-7.776ZE-05
	-2 06.26E-02	1.14656 000	2.0568E-02	1.1168E+00	1.0706E+00	4.8562E-01	-2.9716E-01	-2.2 03 SE- 04
110	20-30546-2-	1.12236400	2.4908E-02	1.0688E+00	1.0431F+00	5.0201E-01	-2.4786E-01	-2.1315E-04
113	20-11925-02	1.00855+80	2.694.2E-112	1.0215E+00	1.0164E+00	5.1824E-01	-1.9931E-01	-1.9 tekt- 04
121	20 36314.2-	1.0763F +0.0	2.6644E-02	9.7768E-01	9.9184E-01	5.3332E-01	-1.5462E-01	-1.05466-04
171	100000000000000000000000000000000000000	1 05535400	2.3978F-02	9.3600E-01	9.6 973E-01	5.4770E-01	-1.1176E-01	-1.25t0t-04
100	11.60322-02	1.0367F+00	1.9594E-02	8.9915E-01	9.4848F-01	5.6042E-01	-7 -41 USE -02	200000
163	30-30-01-1	4 02425486	1-4473F-02	8.6839E-01	9.3172E-91	5.7102E-01	-4.2756E-02	-7.5891E-75
124	-1-4/90E-03	00432777		1.1839E+00	1.1096E+00	4.6280F-01	-3.6635E-01	-1.9991E-U4
355	-1./1945-02	100000000000000000000000000000000000000	6.9217F-03	1-1313E+00	1.0788E+00	4.8075F-01	-3.1183E-91	-1.8151E-U4
129	-1.562/E-UZ	1 1 26 35 400	1.2217E-02	1.0767E+00	1.0473E+00	4.9947E-01	-2.5545E-01	-1.4796E-04
151	1.2631-02	0043600	1.4947F-02	1.0222E+60	1.0165E+ 00	5.1817E-01	-1 - 9948E-01	-1.1853E-04
150	- 1. 3003E-02	1.0737F +00	1.5079E-02	9.7244E-01	9.8868E-01	5.3528E-01	-1.4858E-01	-7.8693E-US
123	20-320711-	1.04928480	1.2646E-02	9.2390E-01	9.61 88E-01	5.5199E-01	-9.9037E-02	-7.9594E-05
130	- 0.14C3E-03	1.0271F+10	9.5853E-03	8.7994 E-01	9.3790E-01	5.6713E-01	-5.4332E-02	- 1.4 97 9E- U2
127	-2.44485-03	1.2133F+00	-2.1767E-02	1.2494E+ 30	1.1489E+00	4.4045E-01	-4.3507E-01	-1.19595-04
133	-4.0955E-03	1.1860E+00	-1.2491E-02	1.1952E+00	1.1163F+00	4.58935-01	-5. / 62 UE-31	
134	-5.0475E-03	1.1581E+00	-4.3002E-03	1.1398E+00	1.0837E+00	4.7757E-01	-2.6116E-01	2.0 592E-05
135	-5.1725E-03	1.1291E+00	1.6698E-03	1.0823E+00	1.02156400	5 1503E-01	-2-0886E-81	8.3625E-05
136	-4.6113E-03	1.1035E+00	3. 9567E-03	1.0315E+00	1.0215E+00	5.4191E-01	-1.2889E-01	-2.533E-05
137	-3.9674E-03	1.0641E+00	Z-2020E-23	9.0337E-01	9.4543F-01	5.6235E-01	-6.8393E-02	-8.7 853E-05
138	-3.2514E-03	1.0341E+00	3. 559 CE -0 5	1.3138F+00	1.1889E+00	4.1835E-01	-5.0419E-01	-1.3438E-05
139	1 -4655 -02	1 24745400	-4-4075F-02	1.2568E+00	1.1537E+C0	4.3775E-01	-4.4353E-01	-1.0540E-05
141	7 02155-02	1.1884F+00	-2.3234E-02	1.1999E+00	1.1193E+00	4.5721E-01	-3.8350E-01	3.5195E-U5
141	C. LERRE-17	1.1485F+00	3,3119E-02	1.1207E+00	1.0727E+00	4.8437E-01	-3.0090F-01	-5.1012E-U5
143	3.0369E-03	1.0942E+00	-1. 82 8E-02	1.0130E+60	1.0113E+00	5.2133E-01	-1.9007E-01	-2 44535-04
177	7.25625-04	1.0612E+00	-8.4602E-03	9.4773E-11	9. 74 94E-01	5.4382E-01	-1.2322 -01	-4 4 66 65 - NA
145	-6.8367E-04	1.0356E+00	-3.4 706E-03	8.9728E-01	9.4727E-01	5.6118E-01	70-36-07-	4 27835-04
146	3.2045E-12	1.2008E+00	-6.4700F-02	1.2245E+00	1.1358E+00	4 .4 7R2E-01	-4-12935-01	6.5112F-05
147	2. 6497E-02	1.1805E+00	-5. 8387E -02	1.1842E+00	1.1115E+00	4. 61 72t -U1	10.000	-4 7011E-06
7	2.0741E-02	1.1448E+00	-5.0041E-02	1.1134E+00	1.0696E+00	4.8617E-01	10-31 126-2-	-4
149	1.4916E-02	1.1051E+00	-4-1342E-02	1.0347E+00	1.0243E+00	5.13416-31	10-37E-01	-2.7 A75E-06
150	9.5489E-03	1.0733E+00	-2.8778E-02	9.7163E-91	9.8854E-01	5.35372-01	1. 4030C-01	-1.2616E-04
151	5.2425E-03	1.0508E+00	-1.8267E-02	9. 2697E-01	9.6365E-UI	10-36506.6	200001	-4.0700F-05
152	1.9950E-03	1.0276E+00	-1.0672E-02	8.8098E-01	9.3848E-01	5.06/4E-31	-1.816.E-01	1.0152E-03
153	4.3111E-02	1.0871E+00	-7.8195E-02	10 - 36.86 - 01	10-369 FD -T	S. 3961F-01	-1.3598E-01	2.4661E-04
154	3.5599E-02	1.0649E+00	-7.3574E-02	9.55016-01	9.0169F-01	5.4526E-01	-1.1915F-01	2.481 AE - 04
155	2.7545E-02	1.05736+00	- P. 3334E-E	30 3 300E - 0 4				

100		*	- 05	1	ž	- [5	- 64	+0-		5	10-	10-	-	-	-04	10-		-	1 26	
2.1 SALF	1	1 . 1 2 65E	R.4.707F	110000	-3.6764E	4.2474E	1.9739E	2.3865E		7. 37 BE	2.9171E-04	1.5628E	2000	1 100E	2.122₹	1.8345E	-	1.009CE	1.6841E	
-1 - 0 7 k OF - 6 1	79 70 4 17 07	-8.3598E-02	A 07445-02	30 37 100	7.4024E-03	-2.9384E-04	-2 .9389E-03	-2-1355F-02	100 1100	-3.5835E-C5	1.6035E-01	1.2414E-01		7 .1115E-WC	3.1666E-02	2 .576 DE-01		1.50//E-01	8.7436E-02	
10-24-0-3	TOLITETOL	5.5718E-01	E STOLE-84	TO 346 40 . C	5.8799E-01	5.8540E-01	5.8459F-01	5.7827F-04		5.7337E-01	6. 3943F-01	6.2740F-01		6.0 955E-01	5.9621E-01	6.7211E-01		6.5659E-01	6.1506E-01	
17-202-0	79-3660006	9.5361E-01	A 44 725-84	70-326 The6	9.0510E-81	9.0916E-01	9-1056E-01	Q 2 8 7 2 F = 8 1	40 1100	9.2802E-01	8.2549 E-01	A-14-00F-01		6.7159E-01	8.9229E-01	7.75315-01		8.3016E-01	8.63 95E-01	
-	9.3007E-31	9.8780E-51		20 07 07 L U I	8-1102E-01	A. 2095E-01	A.2551F-01	A 1610F .01	TA 16 TO	8.6047E-01	6.5632E-01	6. 9876F-11	***	7.5275E-01	7. 92 98E-61	5.6516F-01	-	6.7310E-01	7.3739E-01	
	20-34169-4-	-3.4494E-02		-C-2962-1C	-8.9347E-02	-7.5309F-02	-6. ngakE-82	20 37776 4	38-34001 ·	-3.6052E-02	-9-8926F-02	-6. 513E-02	300000	-5.2963E-82	-4-3205E-02	-E. 2291E-82	70.746.756	-5.1771E-02	-4.3141E-02	
	1.523E+03	1.04115+30		1 • 0 50 0E • 0 0	9. 923 DE-D1	9-97415-81	0 00645-01	19-31066-6	7 • C 0 9 3 C 4 0 0	1.0172E+00	0.14295-01	O ZELLEON	Taraccosc	9.6292E-01	9.8321F-01	A 68775-01	19 100000	9.2276E-01	9.5518E-01	
4	1.97145-02	1-2761F-02	10 100 100	7.9212E-03	4.6137F-62	7 788 AF - 82	200000000000000000000000000000000000000	20 2000000	C.18 /9E-02	1.4715E-02	4 32425-02	A DEVENTED A	30-36/06-6	2, 9225E-02	2.2735F-02	7 777F-03	30111110	3.2463E-32	2.6823E-02	
1	156	157		158	159	450	100	101	195	163	166	101	107	166	167		007	169	170	

 $C_{\rm p}$  for 6% Thick Circular Arc ( $M_{\infty}$  = 0.909)

	•	•	•	•	•	•
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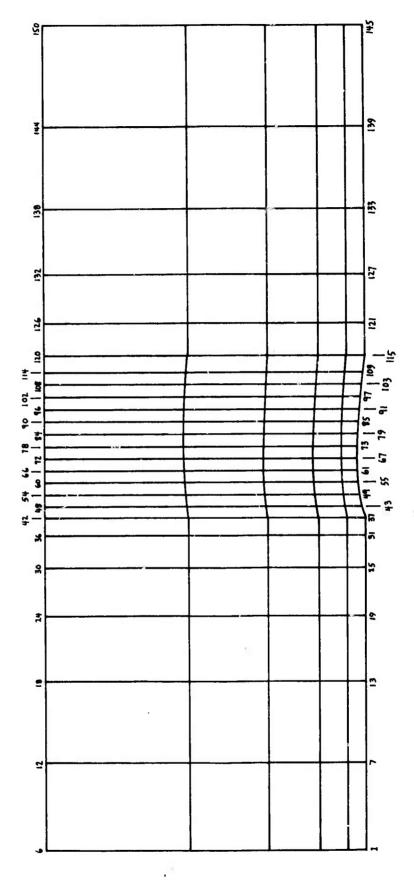


Figure 7 - Freehand Sketch of Finite Element Mesh for NACA 64 A006 Airfoil

The cases to be computed are:

$M_{\infty} = 0.825$	(Subcritical)
$M_{\infty}^{\infty} = 0.875$	(Barely Critical)
$M_{\infty} = 0.900$	(Supercritical)
$M_{\infty} = 0.940$	(Definite Supercritical)

INPUT CARDS TO STRANL-I FOR NACA 64 A006 STEADY TRANSONIC FLUW--NACA64A006--MESH 5 150 NODES

																													i	10.4	145			115	4	
			00	00	00	00	000	000	000	000	00	00	00	00	00	8	00	00	000	000	000	• 000	000	000	000	000	000		•	84	144			109	-0.0174	
			2.000	2.000	2.000	2.000	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.000	2.0	2•0	•	2.0	6	2.0	•	•	2.0		1	42	138			103	44	<b>636</b>
			000	00	00	00	00	00	00	75	20	225	300	75	50	25	00	75	50	25	00	00	00	200	006	400	000			36	132			26	0.0044	-0.0536
			0	0.500	1.000	1.400	1.700	1.900	2.000	2.075	2.150	2.5	2.3	2.375	2.4	2.5	2.6	2.6	2.750	2.8	2.9	3.0	3.2	•	3.0	•	5.0			30	126			6	20	989
	30		00	00	00	00	00	00	00	584	283	557	968	986	945	739	.02438	048	602	•01126	990	00	00	00	၁၀	• 000	000			24	120		139	<b>8</b>	0.0220	-0•0636
	7		0.000	00000	00000	00000	0.000	00000	00000	.01684	.02283	.02657	•02896	.02988	.02945	•02739	•05	.02048	•01602	•01	•0000	00000	00000	00000	0.000	0.0	0			18	114		133	73	00	989
	7		00	00	00	8	00	00	0	75	20	25	0	75	20	525	00	675	20	25	006	00	200	500	006	400	000			12	108		127	73	0.0400	-0.0636
	N		00000	0.500	1.000	1.400	1 • 700	1.900	2.000	2.075	2.150	2.22	2.300	2.375	2.450	2.5	2.600	2.6	2.750	2.825	2.9	3.000	•	3.5	3.9	4 • 4	٥ ٥			9	102		121	67	38	622
4	9			_				_		_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	•	0	0			ល	96		31	61	0.0638	-0.0622
	7		1.70	1.70	1.70	1.70	1.70	1.70	1.70	1.70	1.70	1.70	1.70	1.70	1.70	1.70	1.70	1.70	1.70	1.70	1.70	1.70	1.70	1.70	1.70	1.70	1 • 7(			4	90		52	55	040	562
	54	ırd)	-	7	-	-	-	-	-	7	7	-	_	-	-	-	-	-	-	-	-	-	-	-		-	-	Card)	14	ო	96	150	19	74	0-104	-0.0562
	Ω	Blank Card)	9	9	9	9	9	9	9	9	9	9	9	9	9	9	9	9	9	9	9	9	9	9	9	9			o	Ŋ	78	149	13	43	o	•0465
	4	(Bl	-	1	13	19	25	31	37	43	64	S	61	67	73	79	9	6	76	103	109	115	121	127	133	139	145	(Blank	35	-	72	148	7	37		Ò

 -0.0344

## INPUT CARDS TO STRANL-II FOR NACA 64 A006

```
STEADY TRANSONIC FLUW--NACA64A006--MESH 5 --M=0.825
       (blank card)
                0.825
                         1.000
   6 0.005
         (Insert cards generated in STRANL-I)
STEADY TRANSONIC FLUW--NACA64A006--MESH 5--M=0.675
                           0.500
   12 0.01
                0.875
STEADY TRANSUNIC FLUW--NACA64A006--MESH 5--M=0.900
                 0.90
                           0.500
   12 0.01
STEADY TRANSUNIC FLUW--NACA64A006--MESH 5--MEO.940
                          0.400
   16 0.01
               0.740
```

MACH NUMBER . 940 RELAX. FACTOR = .4666

N005								
	PHIT	NCON	ACOM	<b>400</b>	LMAC	04/4	•	
		0100000		A. A 36.0 E-0.1	9.4000E-01	. 65 785-0	.0-	•
	, ,	9 6		4. A MABE-01	9. 4 60 BE-01	5.65785-01	-0-	•
	•	9		A. A. 35.3 E-0.1	9. + 60 0E - 01	5.65785-01	-0-	•
	•	10000 T	•	A. 4 36.35-0.4	9-46005-01	5.6578E-11	-9.	G
			• 17	A. A 36.0E-0.1	9. 4000E-J1	5.65785-01	-0-	•
		T- FOOD T	•	A-1 MARE-111	9-4-00 CE-01	5.6578E-01		- 1
		1-00000-1	•	A. A 54. 95-01	9.46785-01	5.6528E-01	-1.4338E-33	1.7269E-05
	.7541E-u	1.666/2+66	0 40305-05	A.A 54 7 F-0 1	9. 408 2E-01	5.6526E-01	1843E-1	۰
	.3097E-0	1.000	2 - C 2 2 2 E - D 4	3. 4 SES E-11 1	9-4197E-01	5.65105-01	1349F-0	3444E
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	-4.3859E-U2	9-1973E-01	0.7440E-UZ	2000	A 016 TE-01	5.9676F=B1	9-1108E-02	-4.7 993E-04
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Appendix A
FORTRAN LISTING OF STRANL-I

## Appendix A

A FORTRAN listing of the source deck for the STRANL-I program is presented in the following pages. The program, as presently configured, required 428K words to execute.

```
PROGRAM MAIN(INPUT=65.0UTPUT=131.PUNCH=65.TAPE5=1NPUT.
           TAPE6=OUTPUI)
C
      GENERATE 2-D MESH CONSISTING OF TRIANGLES AND QUADRILATERALS
C
      THE PRESENT PROGRAM HAS TWO OPTIONS
      10PT(11)=1 RENUMBER NODES TO YIELD SMALLER BANDWIDTH
C
                    CALL MPLUT TO PLUT GENERATED MESH
C
      10pT(12)=1
C
      THE PROGRAM AS PRESENTLY DIMENSIONED ALLOWS THE FOLLOWING MAXIMA
C
      200 ELEMENTS, 180 NODES, 10 CONNECTING NODES TO ANY NODE.
C
      50 NODES FOR EACH TYPE OF BOUNDARY CONDITIONS
C
      DEVELOPED AND CODED BY STEVENS CHAN OF LOCKHEED-HUNTSVILLE. ALA.
C
      EXCEPT SUBROUTINE MPLOT WHICH IS CODED AND SUPPLIED BY
C
      CAPT. GERRY VANKEUREN OF AFFDL. WRIGHT-PATTERSON AIR FORCE BASE
      DIMENSION TITLE(8) . 10PT(20) . NDEL(200.4) . MEMUT(1800)
      UIMENSION X(180),Y(180),TUINT(180),NEWJT(180),JOINT(180),JMEM(180)
      DIMENSION NIDS(3) + NID (3+50) + VAF (50)
      EQUIVALENCE (NIDS(1) + NFARF) + (NIDS(2) + NWAKE) + (NIDS(3) + NBODY)
      DATA NEM . NPM . NCN . NEMN/200 . 180 . 10 . 1800/
      READ AND GENERATE MESH INFORMATION .ETC.
C
   10 READ(5.805)(TITLE(1).1=1.8)
      1F(EOF(5))2000,50
   DO CONTINUE
      READ(5.820)(IUPT(1).1=1.20)
      CALL MESHBW (NEM , NPM . NDEL . X . Y . NELS . NPS . MAXN)
C
      READ BOUNDARY NODES AND AIRFOIL SLOPE
      READ 825. NIDS
      DO 120 1=1.3
      NS=NIDS(1)
  120 READ 825. (NID(I,J),J=1.NS)
      READ 830. (VAF(I).I=I.NBODY)
C
C
      EXECUTE NODE RENUMBERING AND MESH PLOT OPTIONS
      1F (10PT(11) •EQ• 1) GO TO 140
      DU 130 1=1.NPS
  130 NJNT(1)=1
      GO TO 150
  140 CALL OPTM(NPM+NEM+NPS+NELS+4+NCN+NEMN+MEMJT+NEWJT+JO1NT+
                 JMEM, NDEL , NUNT , MAXN)
  150 CONTINUE
      IF (10PT(12).EQ.1) CALL MPLOT(X.Y.NDEL.NPM.NEM.NELS.NPS)
C
C
      COMPUTE FULL BANDWIDTH AND PRINT OUTPUT DATA
C
      NEW=6*(MAXN+1)
      PRINT 910. (TITLE(1).1=1.8)
      PRINT 820+ (IUPT(1)+1=1+20)
      PRINT 920. NELS. NPS. NBW
      PRINT 930
      DU 220 N=1 . NELS
  220 PKINT 825. N. (NUEL (N. J) . J=1.4)
      PRINT 935
      DO 230 1=1.NPS
  230 PRINT 940. 1, NJNT(1).X(1).Y(1)
      PRINT 951. (NID(1.1).1=1.NFARF)
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PRINT 952 (NID(2.1) . I=I . NWAKE)
      PRINT 953. (NID(3.1).1=1.NBODY)
      PRINT 955. (VAF(I).I=1.NBODY)
C
C
      PUNCH OUTPUT DATA TO BE USED AS INPUT TO STRANL -- II
C
      PUNCH 825. NELS. NPS. NBW. (NIDS(1).1=1.3)
      PUNCH 825. ((NDLL(I.J).J=I.4).I=I.NELS)
      PUNCH 840 (X(1) + Y(1) + I = I + NPS)
      DO 350 I=1.3
      NS=NIDS(I)
  350 PUNCH 825. (NID(1.J).J=1.NS)
      PUNCH 840 (VAF(I) . I = I . NBODY)
      PUNCH 825. (NUNT(1).1=1.NPS)
      GO IO IU
  805 FORMAT (7A10, A2)
  820 FORMAT(4012)
  825 FURMAT (1615)
  830 FORMAT (8F10.0)
  840 FORMAT (1P8E10.3)
  910 FORMAT(1HI+2X+7A10+A2//)
  920 FORMAT (IHO,-NO. OF ELEMENTS=1.14.1 NO. OF NODES=1.14.
     1
              .
                   FULL BANDWIDTH= 1 + 14//)
  930 FORMAT ('OELE. NO. AND ELEMENT NODES'/)
  935 FORMAT ( ! OOLD NODE ! . . NEW NODE ! . 6X . ! X(1) ! . 12X . ! Y(1) ! / )
  940 FORMAT (16.110.2E15.5)
  951 FORMAT ('ONODES AT FARFIELD'/(2015))
  952 FORMAT ('ONODES UN LINE OF SYMMETRY'/(2015))
  953 FURMAT ('ONODES ON THE AIRFOIL'/(2015))
  955 FURMAT ( OSLUPE ALONG NODES ON AIRFOIL / (8EI5.5))
 2000 STOP
      END
```

```
SUBROUTINE MESHBW (NEM .NPM .NDEL .X .Y .NELS .NPS .MAXN)
C
С
      GENERATE MESH INFORMATION INCLUDING ELEMENT NODE ARRAY.
С
      NODAL COORDINATES. AND MAX. DIFFERENCE IN NODES
C
      DIMENSION NDEL (NEM . 4) . X (NPM) . Y (NPM)
      DIMENSION IDUMP (4) DUMP (4)
 1020 FURMAT(1615)
 1150 FURMAT (315.5F1().0)
C
      GENERATE ELEMENT NODE NUMBERS AND THEIR MAXIMUM DIFFERENCE
С
      DO 100 N=1 . NEM
      DO 100 J=1.4
  100 NDEL(N.J)=0
      NELS = 0
      MAXN=0
  120 READ 1020. NPL.KEI.KEJ.KDI.KDJ.(IDUMP(1).1=1.4)
      IF (NPE . EQ. 0) GO TO 129
      J1=-KDJ
      DO 124 J=1 .KEJ
      J1 = J1 + KDJ
      J2 = J1 - KDI
      DO 124 I=1 .KEI
      NELS = NELS + 1
      J2 = J2 + KDI
      DO 124 K=1.NPE
  124 NDEL(NELS+K) = IDUMP(K) + J2
      DO 126 1=1.NPE
      DO 126 J=1 .NPE
      NDIFF=NDEL(NELS.I)-NDEL(NELS.J)
  126 IF (IABS(NDIFF) .GT. MAXN) MAXN=IABS(NDIFF)
      GO TO 120
  129 IF (NELS .GT. NEM) GO TO 300
C
      GENERATE NODAL COORDINATES
C
С
      READ 1020 NPS
  130 READ 1150. ND.NNI.NDI.RATIO. (DUMP(I).I=1.4)
      1F (ND .EQ. 0) GO TO 140
      TEMP2 = 1.0
      IF (NN1 .LT. 3) GO TO 135
      J1 = NNI - 1
      TEMP1 = 1.0
      TEMP2 = 0.0
      DO 134 I=1.J1
      TEMP2 = TEMP2 + TEMP1
  134 TEMP1 = RATIO*TEMP1
  135 TEMP1 = (DUMP(3)-DUMP(1))/TEMP2
      TEMP2 = (DUMP(4)-DUMP(2))/TEMP2
      JI = ND
      TEMP3 = 0.0
      TEMP4 = 0.0
      DO 137 I=1.NNI
      X(J1) = DUMP(1) + TEMP3
      Y(J1) = DUMP(2) + TEMP4
      JI = JI + NDI
      TEMP3 = TEMP3 + TEMP1
```

TLMP4 = TEMP4 + TEMP2

TLMP1 \* RATIO\*TEMP1

11/ ILMP2 \* RATIO\*TEMP2

GO TO I30

140 IF (NPS \*GT\*\* NPM) GO TO 400

RETURN

PRINT ERROR MESSAGE IF DIMENSIONS FOR ELEMENTS OR NODES EXCEEDED

300 PRINT 310\*\* NELS\*\*NEM

310 FORMAT (\*OTOO MANY ELEMENTS\*\*\*SX\*\*\*NELS=\*\*I4\*5X\*\*\*NEM=\*\*I4)

CALL EXIT

400 PRINT 410\*\* NPS\*\*NPM

410 FORMAT (\*OTOO MANY NODES\*\*\* 5X\*\*\*NPS=\*\*I4\*5X\*\*\*NPM=\*\*I4)

CALL EXIT

END

```
SUBROUTINE OPTM(NPM.NEM.NPS.NELS.NPE.NCN.NEMN.MEMJT.NEWJT.
          JOINT . JMEM . NUEL . NUNT . MAXN)
      RENUMBER THE NOVES TO REDUCE BANDWIDTH. WITH NUNT CONTAINING THE
C
      NEW NODAL NUMBERS (LOCATION IN ARRAY REPRESENTS THE OLD NODAL NO.)
      NPM=MAX. NO. UF NODES. NPS=ACTUAL NO. OF NODES
C
      NEM=MAX. NO. UF ELEMENTS. NELS=ACTUAL NO. OF ELEMENTS
C
      NPE=MAX. NO. UF NODES AMONG ALL THE ELEMENTS
C
      NCN=ESTIMATED MAX. NO. OF NODES CONNECTED TO ANY NODE
C
      NUEL = ELLMENT NOVE POINTS
C
      MAXN=MAX. DIFF. BETWEEN NODAL POINTS IN ANY ELEMENT
C
      MEMUT. NEWJT. JOINT. JMEM ARE INTERMEDIATE WORKING SPACE
C
C
      DIMENSION NDEL(NEM.NPE).NUNT(NPM).MEMUT(NEMN)
      DIMENSION NEW JT (NPM) . JOINT (NPM) . JMEM (NPM)
C
      ESTABLISH NODES CONNECTED TO EACH OF THE NODAL POINT
      DO 10 J=1.NPS
   10 JMEM(J)=0
      DO 60 J=1 . NELS
      DO 50 I=1 NPE
      JNT I = NDEL (J. I)
       IF (JNTI .EQ. 0) GO TO 60
      JSUB=(JNTI-I)*NCN
      DO 40 11=1 . NPE
                       GO TO 40
       IF (II •EQ• I)
       JJT=NDEL(J+II)
       IF (JJT .EG. 0) GO TO 50
       MEMI = JMEM (JNTI)
       IF (MEMI .EQ. 0) GO TO 30
       DO 20 111=1.MEM1
       JP=JSUB+III
       IF (MEMUT(JP) .EQ. JJT) GO TO 40
    20 CONTINUE
    1+(ITAL)MAML=(ITAL)MAML OE
       NPOS=JSUB+JMEM(JNTI)
       MEMUT (NPOS) = JUT
    40 CONTINUE
    50 CONTINUE
    60 CONTINUE
       DO 100 1=1 . NPS
       IF (JMEM(1) .LE. NCN) GO TO 100
       PRINT 90. I.NCN
    90 FORMAT ( OERRUR ... NODE ! . 15 . HAS MORE THAN ! . 15 . CONN . NODES ! )
       CALL EXIT
   100 CONTINUE
 C
       THE ORIGIN OF THE NEW NUMBERING SYSTEM IS LOCATED AT EACH NODE
 C
       IN TURN TO SEARCH FOR THE ONE WITH SMALLEST BANDWIDTH
 С
 C
       DO 160 IK=1.NPS
       DO 120 J=1 .NPS
        U=(L)TNIOL
   120 NEWJT(J)=0
       MAX=0
        I = I
       NEWJT(1)=1K
```

JUINT(IK)=1 K=1 130 NEW=NEWJT(1) K4=JMEM(NEW) IF (K4 .EQ. 0) GO TO 145 JSUB=(NEWJT(I)-1)\*NCN DO 140 JJ=1.K4 JP=JSUB+JJ K5=MEMJT(JP) IF (JCINT(K5) .GT. 0) GO TO 140 K=K+1 NEWJT(K)=K5 JOINT (K5) = K NDIFF=IABS(I-K) IF (NDIFF .GE. MAXN) GO TO 160 IF (NDIFF .GT. MAX) MAX=NDIFF 140 CONTINUE 1F (K .EQ. NPS) GO TO 150 145 I=1+1 GO TO 130 150 MAXN=MAX DO 155 J=1 .NPS 155 NUNT(J)=JOINT(J) 160 CONTINUE RETURN END

```
SUBROUTINE MPLUT(XC+YC+NODE+NN+NE+NELS+NPS)
C
      USE CALCOMP PLOTTER TO PLOT GENERATED MESH
C
      CUDED BY CAPT. GERRY VANKEUREN OF AFFUL. WRIGHT-PATTERSON AFE
C
C
      DIMENSION XC(NN), YC(NN), NODE (NE, 4), XP(7), YP(7)
      DEFINE PLOT SIZE AND PLACE PEN IN INITIAL POSITION
C
      DU 5 L=1.NPS
      XC(L)=XC(L) *8.
    5 YC(L)=YC(L) *8.
      CALL PLOT(0.0,-3.0,-3)
      CALL PLOT(1.0.3.0.-3)
      DRAW EACH ELEMENT IN TURN
C
      DO 10 1=1.NELS
      NPE=5
       IF (NOUL(1.4).EU.0) NPE=4
      NPP=NPE-1
      DO 9 J=1.NPP
      XP(J)=XC(NODE([,J)))
    9 YP(J)=YC(NODE(I,J))
      XP(NPE) = XP(1)
       YP(NPE)=YP(1)
       XP(NPE+1)=YP(NPE+1)=0.0
       XP(NPE+2)=YP(NPE+2)=1.0
   10 CALL LINE (XP, YP, NPE, 1,0,0)
       WRITE NODAL NUMBERS AND FINALLY END THE PLOT
       DU 20 L=1 . NPS
       PL=FLOAT(L)
    20 CALL NUMBER (XC(L) . YC(L) . . 14 . PL . 0 . - 1)
       CALL PLOTE
       RETURN
       LND
```

Appendix B
FORTRAN LISTING OF STRANL-II

## Appendix B

A FORTRAN listing of the source deck for the STRANL-II program is presented in the following pages. The program, as presently configured, requires 177<sub>8</sub>K words to execute.

```
PROGRAM MAIN(INPUT=65.0UTPUT=131.PUNCH=65.TAPE5=INPUT.
          TAPE6=OUTPUT)
      STEADY TRANSUNIC FLUW ANALYSIS BY FINITE ELEMENT METHOD
Ċ,
      USING LEAST SQUARES WITH TRIANGULAR AND QUADRILATERAL ELEMENTS
      TUPT(1)=1. USE RESULTS OF PREVIOUS CASE AS STARTING SULUTION
      WHILE THE UTHER UPTION IS IGNURED
      10P1(2)=1. READ IN NON-ZERO INITIAL GUESS
Ċ
      IUPT(3)=1. APPLY LINEARIZED BOUNDARY CONDITION ON CHORDLINE
      THE PROGRAM AS PRESENTLY DIMENSIONED ALLOWS THESE MAXIMA
      200 ELEMENTS . 100 NUDES . 50 NUDES FOR EACH TYPE OF BOUNDARY COND.
      MAX. FULL MANINIDTH = 84
      DEVELOPED AND CODED BY STEVENS CHAN OF LUCKHEED-HUNTSVILLE ALA.
      DIMENSIUM TITLE (8) . TOPT (20) . NCD (200 . 4) . 5 (540 . 84) . 5 EP (540)
      DIMENSION A(180) , Y(180) , RML(180) , RMLP(180) , COF (180) , NSNT(180)
      DIMENSION NIDS(3) . NID(3.50) . VAF(50) . AR(100)
      LUGICAL LK (50)
      EGUIVALLINCE (NIUS(I) + NFARF) + (NIUS(2) + NWAKE) + (NIUS(3) + NBODY)
       DATA NEM . NPM . NCM . NA/200 . 180 . 84 . 50/
      DATA P1/3.1415926/.GAMMA/1.40/
      MKM=3*NPM
       14=2*NA
       CUNST=0.5* (GAMMA-1.0)
       EXP=-GAMMA/(GAMMA-1.0)
       READ TITLE . CUNTRUL KEYS . AND PRUBLEM PARAMETERS
   100 READ(5.005) (TITLE(1).1=1.8)
       IF(EUF(5))2000,101
   101 CUNTINUL
       KEAD (5.820) (IUP [(1):1=1:20)
       READ 630. ITGIV: ZIEST . RMAC. FI
       PRINT 910. (TITLE(1). I=1.8). ZIEST
       PRINT 820 (1UP1(1) 1=1 20)
       IKES=0
       KF T = 1 . 0
       SUMAC=RMAC**2
       IF (10PT(1) .Lu. 1) GO TO 382
       READ AND PRINT MESH DATA. BOUNDARY MODES, AND AIRFUIL SLUPE
       READ 825. NELS, 12PS. NBW. (NIUS(1), 1=1.3)
       KLAU 825. ((NUD([.J).J=1.4).I=1.NELS)
       READ 840. (X(I).Y(I).I=I.NPS)
       DU 110 1=1.3
       N5=N1D5(1)
   110 READ 825. (NIU(1,J).J=1.NS)
        READ 840. (VAF(1).1=1.NBODY)
```

```
120 READ 825. (NJNT(1) . 1=1.NPS)
      IF IOPT(3)=1, APPLY LINEARIZED BOUNDARY CONDITION ON CHORDLINE
C
      OTHERWISE APPLY NUMBERAR BOUNDARY CONSITION ON AIRPOIL SURFACE
C
      1+ (10PT(3) .NE. 1) GO TO 116
      DO 115 A=1. WRODA
      1=NID(3.J)
  115 Y(1)=0.0
  116 CONTINUE
  200 PRINT 920. NELS.NPS.NBW
      PHINT 930
      DO 220 N=1 . NELS
  220 PRINT 825 + N. (NUD(N.J).J=1.4)
      PRINT 935
      DO 230 1=1.NPS
  230 PRINT 940. I.NJNT(1).X(1).Y(1)
      PRINT 951. (NID(1.1). I=1.NFARF)
      PRINT 952. (NID(2.1).1=1.NWAKE)
      PRINT 953. (NID(3.1).1=1.NGODY)
      PRINT 955. (VAF(I).I=1.NBODY)
C
      REDEFINE MESH DATA. ETC. USING NEW NODAL NUMBERING SYSTEM
C
      DO 238 N=1 . NELS
      DU 238 1=1.4
      IF (NOD(N+1) .EU. 0) GO TO 238
      KK=NOD(N+1)
      NOD(N+1)=NJNT(KK)
  238 CONTINUE
      DU 239 1=1.3
       IS=NIDS(I)
      DO 239 J=1.15
      KK=NID(I.J)
  239 NID(I+J)=NJNT(KK)
       DO 243 1=1.NPS
       RMLP(I)=X(I)
  243 RML(I)=Y(I)
       DO 244 II=1.NPS
       I = NJNT(II)
       X(I) = RMLP(II)
  244 Y(1)=RML(11)
C
       HALF BANDWIDTH AND NUMBER OF EQUATIONS
C
C
       NHBW=NBW/2
       NEQ=3*NPS
       READ NONZERO INITIAL GUESS OR PROCEED WITH ZERO SOLUTION
C
C
       IF (IOPT(2) .NE. 1) GO TO 250
       READ 840+ (S(I+NBW)+1=I+NEQ)
       GU TU 295
   250 DO 260 1=1 NEW
   260 SLP(1)=0.0
C
       ITERATIONS START HERE AND CHECKED IF ITGIV IS EXCEEDED. IF SO.
C
       PRINT FAIL TO CONVERGE AND PROCEED TO NEXT CASE. OTHERWISE.
```

```
CONTINUE TO LIERATE
   205 IRES=IRES+I
       IF (IRES .GT. ITGIV) GO TO 600
       FORMULATE SYSTEM OF ALGEBRAIC EQUATIONS
       DU 266 1=1 . NEW
       DU 266 J=1 , NBW
   206 5([.J)=0.0
       CALL NEWN (SQMAC , NRM . NCM . NEW , NEW . NEW . NELS . NOD . SLP . S . COF . NPM . X . Y )
       IMPOSE D. C. FOR FARFIELD. LINE OF SYMMETRY. AND ON AIRFOIL
 C
       00 274 I=1 .NFARE
       IE=3*N1U(1.1)-3
       DU 272 II=1.3
       IE=1E+1
       DU 270 K=1.NBW
   270 S(IE.K)=0.0
   272 S(IE.NHUW) =1.0
   274 CONTINUE
       DU 280 I=1 . NWAKE
       IL=3*N10(2.1)
       DO 278 K=1 .NBW
   278 S(IL.K)=0.0
   280 S(IE . NHEW) = 1 . 0
       DO 285 J=1 . NBUDY
       IE=3*NID(3.J)
       DO 282 K=1.NBW
  282 S(IE.K)=0.0
       S(IE , NHUW) = 1 .0
       1F (10PT(3) .NE. 1) S(1E.NHBW-1)=-VAF(J)
  285 S(IE . NBW) = VAF(J)
       CALL BANDED SULVER TO SOLVE THE SYSTEM OF EGUATIONS
C
       CALL BNDEG (S . NRM . NCM . NEG . NHBW)
C
C
      PRINT COMPUTED RESULTS
  295 PRINT 970. RMAC. RFT
      PRINT 975. IRES
      DO 305 I=1.NPS
      (I) TNUN=L
      II=3*NJNT(I)
      POT=S(II-2.NBW)
      UPT=S(11-1 .NBW)
      V=S(II.NUW)
      U=UPT+1.0
      USQ=U*U+V*V
      ASQ=CONST*(1.0-USU)+1.0/SQMAC
      RML(J)=SURT(USU/ASU)
      PRATIO=(1.0+CONST*RML(J)**2)**EXP
      CP=-2.*UPT
      COF(J)=SQMAC*(1.0+2.4*UPT)
      DELM=RML(J)-RMLP(J)
  305 PRINT 978, 1.POT.U.V.COF(U).RML(U).PRATIG.CP.DELM
C
      DISPLAY PRESSURE COEFFICIENT CP
C
      PRINT 985
      ISTUP=0
      IPNT=0
```

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```
DO 320 J=1.NBUDY
      IF (J .EG. NBUDY) ISTOP=1
      1=NID(3,J)
      UPT=S(3*1-1,NBW)
      V=S(3*1+NBW)
      CP=-2.*UPT
  JEO CALL FPLUT(IA, IPNT. AR. LR. ISTOP. 1.1.X(I), CP)
      IF (IRES .LT. 2) GO TO 382
C
      CHECK CONVERGENCE. IF SO. PUNCH CONVERGED SOLUTION AND
C
      PROCEED TO NEXT CASE. OTHERWISE. UPDATE SOLUTION AND CONTINUE
C
      TO ITERATE
      DU 340 I=1.NPS
      PCTE=1.0-RMLP(I)/RML(I)
      IF (ABS(PCTE) .LT. ZTEST) GO TO 340
      KFT=F1
      GO TO 382
  340 CUNTINUE
      PUNCH 840 (5([ + NBW) . I=1 . NEQ)
      GU TO 100
  382 UO 385 1=1.NPS
  385 RMLP(I)=RML(I)
      RFTC=1.0-RFT
      UO 390 I=1 . NEW
  390 SLP(1)=RFT*S(1,NBW)+RFTC*SLP(1)
      GU TO 265
  600 PRINT 980
      GO 10 100
  805 FORMAT (7410.42)
  820 FORMAT (4012)
  825 FURMAT (1615)
  830 FURMAT (15.3F10.0)
  840 FORMAT (1P8E10.3)
  910 FURMAT(1H1.2X.7A10.A2// CONVERGENCE LIMIT = 1.F6.4//)
  920 FORMAT (1HO,-NO. OF ELEMENTS= 1.14. NO. OF NODES-1.14.
                  FULL BANDWIDTH= 1 . 14//)
  930 FORMAT ( OELE. NO. AND ELEMENT NODES !/)
  935 FORMAT ( + OULD NUDE + + NEW NODE + + 6X + + X(1) + + 12X + + Y(1) + /)
  940 FORMAT (16.110,2E15.5)
  951 FCRMAT ( ONODES AT FARFIELD / (2015))
  952 FORMAT ('ONODE'S ON LINE OF SYMMETRY (2015))
  953 FURMAT ( UNODES UN THE AIRFOIL / (2015))
  955 FURMAT ('OSLOPE ALONG NODES ON AIRFOIL'/(8E15.5))
  970 FURMAT (1H1. -MACH NUMBER= 1.F6.3.5X. TRELAX. FACTUR = 1.F6.4/)
  975 FORMAT (1HU,4A,-NO. OF ITERATION=++14/
     1
               1HO, 7X, -NODE . 8X. PHIT . 11X. UCOM . 11X. VCOM .
             I2X . COF - , 11X . LMAC . . 11X . . P/PU . . 13X . . CP . . 11X . . DELM . / )
  978 FURMAT (110,1P8=15.4)
  980 FURMAT (*OFAIL TO CONVERGE IN SPLCIFIED NO. OF ITERATIONS!)
  905 FORMAT (1H1)
 2000 STOP
      END
```

```
SUBROUTINE NEWK (SOMAC . NRM . NCM . NEW . NEW . NEM . NELS . NOD . SLP . S .
          COEF . NPM . X . Y )
C
      GENERATE SYSTEM MATRIX BY ASSEMBLLING CONTRIBUTIONS FROM
C
C
      ALL THE ELEMENTS
      SUBROUTINE EMGT CALLED TO GENERATE ELEMENT MATRIX
Ç
C
      DIMENSION COEF (NPM) + X (NPM) + Y (NPM) + XQ(4) + YQ(4) + PM(12) + BB(12+12)
      DIMENSION NOU(NEM+4)+5(NRM+NCM)+5LP(NRM)
      NHAW=NBW/2
      DU 480 N=1 . NELS
      11=1
      1F (NOD(N+4)) 402+402+404
  402 NPEL=3
      NTRS=1
      GO TO 410
  404 NPEL=4
      NTRS=4
       12=0
      DO 408 1=1 .4
      NI=NOD(N+1)
  408 IF (COEF(NI) .GT. 1.00)
                                   12=12+1
       IF (12 .EQ. 0) NTRS=2
       1F (12 .EQ. 4)
                        11=3
   410 DO 425 1=1 .NPEL
       NI=NOD(N.1)
       xu(1)=x(N1)
       YQ(1)=Y(N1)
       DO 425 J=1.3
       15=3*(N1-1)+J
       1E=3*(1-1)+J
   425 PM(IE)=SLP(IS)
       CALL EMUT (XQ.YU.PM.SQMAC.BB.NTRS)
       DO 450 1=11.NPEL
       NR=3*(NOD(N,I)-1)
       IE=3*(1-1)
       DO 450 11=1.3
       NH=NR+1
       1E=1E+1
       DO 450 J=1 .NPEL
       NC=3*(NOD(N.J)-1)-NR+NHBW
        JE=3*(J-1)
       DO 450 JJ:1.3
       NC=NC+1
        JE=JE+1
    450 S(NR.NC)=S(NR.NC)+BB(IE.JE)
    480 CONTINUE
        RETURN
        END
```

```
SUBROUTINE EMUTING PMU SUMAC . EQ . NTRS )
C
C
      GENERATE MATRIX FOR A QUADRILATERAL OR TRIANGLE
C
      SUBROUTINE EMTC CALLED TO GENERATE MATRIX FOR A BASIC TRIANGLE
C
      DIMENSION EQ(12+12) .ET(9+9) .XU(4) .YU(4) .XT(3) .YT(3) .MP(3-4)
      DIMENSION PMQ(12) .PMT(9)
      DATA MP/1.2.3.3.4.1.2.3.4.4.1.2/
      FTOR=1.0
      IF (NTRS .EQ. 4) FTOR=0.5
      DO 100 1=1.12
      DO 100 J=1+12
  100 EQ(1.J)=0.0
      DO 150 11=1.NTRS
      DO 105 1=1.3
      N1=MP(1.11)
      1T=3*(1-1)
      14=3*(N1-1)
      DO 102 J=1+3
      IT = IT + 1
      10=10+1
  102 PMT(IT)=PMQ(IQ)
      XT(1)=XU(N1)
  105 YT(1)=YQ(N1)
      CALL EMTC(ET+XT+YT+PMT+SQMAC)
      DO 130 K=1.3
      NR=3*(MP(K+11)-1)
      1E=3*(K-1)
      DO 130 KK=1.3
      NK=NR+1
      IE=IE+1
      DO 130 L=1.3
      NC=3*(MP(L+11)-1)
      JE=3+(L-1)
      DO 130 LL=1.3
      NC=NC+1
      JE=JE+1
  130 EU(NR.NC)=EQ(NR.NC)+ET(IE.JE)*FTOR
  150 CONTINUE
      RETURN
      END
```

The second secon

CST=WEIGHT\*Q(I) DO 60 J=1.9

100 CONTINUE RETURN END

60 A(I+J)=A(I+J)+CST\*P(J)

```
C
      EVALUATE SHAPE FUNCTION DERIVATIVES AT GAUSSIAN POINT
C
C
      DIMENSION B(3) + C(3) + S(3) + DNX(9) + DNXX(9) + DNYY(9) + NP(5)
      DATA NP/1+2+3+1+2/
      TWOA=2. *AREA
      TWOASU=TWUA**2
      DO 200 I=1.3
      J=NP(1+1)
      K=NP(1+2)
      SI=S(1)
      SJ=S(J)
      SK=S(K)
      HI=8(1)
      6J=8(J)
      BK=B(K)
      CI=C(I)
      CJ=C(J)
      CK=C(K)
      SISQ=51*SI
      BISQ=BI*BI
      CISQ=CI*CI
      ALFA=0.5*(CK-CJ)
      BETA=0.5* (BJ-BK)
      HX=BI*SJ*SK+BJ*SK*SI+BK*SI*SJ
      HXX=2.*(SI*BJ*BK+SJ*BK*BI+SK*BI*BJ)
      HYY=2.*(S1*CJ*CK+SJ*CK*C1+SK*C1*CJ)
      CSS=6.*SI*(1.-SI)
      CS=6.*(1.-2.*SI)
      L=3*1-2
      DNX(L)=B1*CSS+2.*HX
      DNXX(L)=BISQ*CS+2.*HXX
      DNYY(L)=C1SQ*CS+2.*HYY
      CS=CK*SJ-CJ*5K
      L=L+1
      DNx(L)=2.*BI*S1*CS+TWOA*SISQ+ALFA*HX
      DNXX(L)=2.*BISQ*CS+4.*BI*TWOA*SI+ALFA*HXX
      DNYY(L)=2.*CISQ*CS+ALFA*HYY
      85=8J#SK-3K#SJ
      L=L+1
      UNX(L)=2.*BI*SI*BS+BETA*HX
      DNxx(L)=2.*BISQ*BS+BETA*HXX
  200 DNYY(L)=2.*CISQ*BS+4.*CI*TWOA*SI+BETA*HYY
      DU 300 I=1.9
      AUMI / (I) XNC = (I) XNC
      DNXX(I)=DNXX(I)/TWOASQ
  300 DNYY(1)=DNYY(1)/TWOASQ
      RETURN
```

SUBROUTINE DERV (AREA + B + C + S + DNX + DNXX + DNYY )

END

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SUBROUTINE BNDEW (A . NRMAX . NCMAX . N . I TERM)
C
      EQUATION SOLVER FOR BANDED NON-SYMMETRIC SYSTEM OF EQUATIONS
C
C
      SULUTION STORED IN THE LAST COLUMN A(1.2*ITERM)
C
      DIMENSION A(NRMAX . NCMAX)
      CERO=1.E-6
      PARE = CERO**2
      NUND=2*ITERM
      NBM = NBND - 1
C
      BEGINS ELIMINATION OF THE LOWER LEFT
      DO 1000 I=1. N
      IF ( ABS(4(I.ITERM)) .LT.
                                  CERO) GO TO 410
      GO TO 430
  410 IF ( ABS(A(1, ITERM)) .LT. PARE)
                                            GO TO 1600
      PRINT 420. A(I, ITERM). 1
  420 FURMAT ( WARNING. ILL-CONDITIONED A-MATRIX. A= 1.E16.6. 1=1.14)
  430 JLAST = MINO(I+ITERM-1. N)
      L = ITERM + 1
      DU 500 J=1. JLAST
      L = L - 1
      IF ( ABS(A(J.L)) .LT. PARE) GO TO 500
      B = A(J.L)
      DO 450 K=L. NBND
  450 A(J+K) = A(J+K) / B
      IF (1 .EQ. N) GO TO 1200
  500 CUNTINUE
      L=0
      JFIRST = 1 + 1
      IF (JLAST .LE. I) GO TO 1000
      DO 900 J= JFIRST, JLAST
      L=L+1
      IF ( ABS(A(J.ITERM-L)) .LT. PARE) GO TO 900
      DO 600 K=ITERM, NHM
  600 A(J*K-L) = A(J-L*K) - A(J*K-L)
      A(J.NBND) = A(J-L.NBND) - A(J.NBND)
      IF (I •GE • N-ITERM+I) GO TO 900
      DO 800 K=1. L
  800 A(J \cdot NBND - K) = -A(J \cdot NBND - K)
  900 CONTINUE
 1000 CONTINUE
      BACK-SUBSTITUTION
 1200 L = ITERM - 1
      DO 1500 1=2. N
      DO 1500 J=1. L
      IF (N+1-1+J .GT. N) GO TO 1500
      A(N+1-I\bullet NBND) = A(N+1-I\bullet NBND) - A(N+1-I+J\bullet NBND)*A(N+1-I\bullet ITERM+J)
 1500 CONTINUE
      RETURN
      PRINT THE ENTIRE MATRIX IF ZERO ON MAIN DIAGONAL
 1600 PRINT 1601
 1601 FURMAT ! COMPUTATION STUPPED IN BNDEG BECAUSE ZERO APPEARED ON
     . JANCDAID NIAMI
                       THE MATRIX FULLOWS. 1)
      DO 1602 I=1. N
 1602 PRINT 1603. (A(1,J). J=1. NBND)
 1603 FURMAT (10E12.4)
      STOP
      END
```

```
SUBROUTINE FPLOT (MI . 1PNT . AR . LR . 1STOP . NC . NCMAX . VI . V2)
C
C
      PHINTER FLOT FOR DISPLAYING COMPUTED RESULTS
C
                  LM(2) . LN(120) . LP(4) . LX(4) . LR(1) . LC(20)
       INTEGER R1(2) . ST(2) . SG(2)
      D1MENSION AR(M1) *N(120) *RHO(30) *2(15) *10FF(2) *15F(2) *5F1(2) *5F2(2)
      1.ID(2).156(2).11(4).1P(4).1M(4).1X(4).1R(802).1A(238)
      EUUIVALLNCL (IP(1) + LP(1)) + (1M(1) + LM(1)) + (LN(1) + N(1) + RHO(1)) +
      1(1x(1)+Lx(1))+(N120+R1(1))+(N58+R1(2))
       DATA (2(1) +1=1,15)/1 - 1 - 25 - 1 - 5 + 1 - 75 - 2 - 2 - 5 - 3 - 3 - 5 - 4 - 4 - 5 - 5 - 6 - 6
      170.80.90/
      DATA (1SP(1) \cdot 1 = 1 \cdot 2) \cdot (IX(1) \cdot 1 = 1 \cdot 4) \cdot (IP(1) \cdot 1 = 1 \cdot 4) \cdot (1M(1) \cdot I = 1 \cdot 4)
      110.5.6.*1HX.4+1H+.4*0/
       DATA 10(1) +10(2) +15G(1) +15G(2)/120+58+1+-1/
       DATA LN(1) + 1 I + LC(1) / 1 + 80 + 50 + 0 + 1 + 1 HO/
       IF(1STOP)173,172,172
  172 J=IPNT+2
       1F(J.GT.M1)GO TU 173
       1PNT=J
       AR(J-1)=V1
       2V=(J) AA
       DO 10 K=1.4
   10 1M(K) = NC
       J=J/2
       LR(J)=LM(2)
  173 1F(NC.LT.NCMAX)RETURN
       1F(ISTOP.EQ.O)RETURN
       DO 171 1=1.2
       R1(1)=1D(1)
       SG(1)=1SG(1)
       IF(11(1) • NE • 0) R1(1) = 11(1)
       1F(11(1+2).EQ.1)SG(1)=-SG(1)
  171 ST(1) = (R1(1)+1-SG(1)*(R1(1)-1))/2
       1F(R1(1).GT.120)R1(1)=120
       1F(R1(2).GT.238)R1(2)=238
       N20 = N123/6
       N120 = 6* N20
       DO 3 1=1.2
       AMIN=AR(1)
       AMAX=AR(I)
       DC 7 J=1.1PNT.2
       AA1=AR(J)
       1F (AMIN.GT.AA1) AMIN=AA1
     7 1F(AMAX+LT+AA1)AMAX=AA1
       IF (ABS(AMIN) .LT. .000001) AMIN = 0.0
       IF (ABS(AMAX) .LT. .000001) AMAX = 0.0
       R=AMAX-AMIN
       1F (ABS(R).LT.1.E-9.AND.AbS(AMAX).LT.1.E-9) R=1.0
       1F (ABS(R)+LT+1+L-9+AND+AMAX+LT+0+)
                                                          R=-AMAX
       1F (ABS(R).LT.1.L-9.AND.AMAX.GT.O.)
                                                          R= AMAX
       DO 22 J=1.15
       B=ALOG10(R/(RI(I)-2)/Z(J))
       M=B
       IF (B.LT.0) M=M-1
       C=Z(J)*10**(M+1)
       B=AMIN/2(J)/10. **(M+1)
```

11=8

```
IF(B.LT.0) 11=11-1
   1F((RI(1)-2+I1)*C-AMIN)18+19+19
18 C=10. *C
19 1F(J.EQ.1)SMIN=C
22 1F(C.LT.SMIN) SMIN=C
   SF1(1)=(1./SMIN) *SG(1)
   B=AMIN/SMIN
   M=R
   1F(B.LT.0)M=M-1
   SF2(1)=ST(1)-M+SG(1)
   HHO(1)=SF2(1)+0.5
   M=SF2(1)
   DO 25 J=1.10
   1F(M-J-((M-J)/[SP(1))*1SP(1))25.3.25
25 CONTINUE
  3 10FF(1)=J
   DO 101 1=1.N58
101 IA(1)=0
    DO 102 J=1, IPNT,2
    IR(J) = SFI(1) * AR(J) + RHO(1)
    1T=SF1(2)*AR(J+1)+RHO(2)
    1F(J.NE.1)GO TO 109
    IR( IPNT+2)=2
    IR(J+1)=0
108 13=IT
    GO TO 102
109 1F(1T-13)104,105,105
104 1R(J+1)=IR(1PNT+2)
    1R(IPNT+2)=J+1
    GO TO 108
105 1=IT+I
106 1=1-1
    11=1A(1)
    IF(11)106+106+107
107 1R(J+1)=IR(11)
    1R(11)=J+1
102 IA(IT)=J+1
    LAST=IPNT+2
    JJ=10FF(2)
    LZH=SF2(1)
    LZV=SF2(2)
    DO 100 I=1 .N58
    DO 40 J=1.N120
 40 N(J)= 1H
    IF((1-1)*(1-N58))140+151+140
151 DO 141 J=1 +N120
141 N(J) = 1X(1)
140 LN(1)=LX(1)
    LN(N120) = -X(1)
    1F(LZH.LE.O.OR.LZH.GT.NI20)GO TO 131
    LN(LZH)=LP(4)
131 NB=1
     IF(1.NE.JJ)G0 TO 35
    NB=2
    JJ=JJ+5
     13=10FF(1)
    DO 32 J=13.N120.10
  32 LN(J)=LP(4)
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IF (I.NE.LZV)GU TO 35
   DO 135 J=1.N120
135 N(J) = IP(1)
35 13=1A(1)
    IF(13.EQ.0)GO TO 121
120 LAST= IR(LAST)
    12= IR(LAST-1)
    11=LAST/2
    LM(2)=LR(11)
    1MM = IM(2)
    LN(12)=LC(IMM)
    1F(LAST.NE.13)GO TO 120
121 GO TO (38.41) NB
 38 WRITE (6+39) (N(J)+J=1+N120)
                     •120AI)
 39 FORMAT(11H
    GO TO 100
 41 AA1=1
    VALUE=(AAI-SF2(2))/SF1(2)
    WRITE(6.42) VALUE , (N(J) , J=1.N120)
 42 FORMAT(1H .1PE10.3.120A1)
100 CONTINUE
    13=10FF(1)
    J=0
    DO 49 I=13.N120.10
    1+L=L
    AA=I
 49 RHO(J)=(AA-SF2(1))/SF1(1)
    IF(10FF(1)-5)62.62.63
 62 WK1TE(6.50) (RHO(1) . I=1.J'
 50 FORMAT(10X.12(1PE10.3))
    RETURN
 63 IF (J.GE.12) J=11
    WRITE(6.64)(RHO(I).I=1.J)
 64 FURMAT(16X+11(1PE10+3))
    RETURN
    END
```

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